

Dynamic Memory Allocation

Zhaoguo Wang

Why dynamic memory allocation?

Do not know the size until the program runs (at runtime).

```
#define MAXN 15213
int array[MAXN];

int main(void)
{
    int i, n;
    scanf("%d", &n);
    if (n > MAXN)
        app_error("Input file too big");
    for (i = 0; i < n; i++)
        scanf("%d", &array[i]);
    exit(0);
}
```

Why dynamic memory allocation?

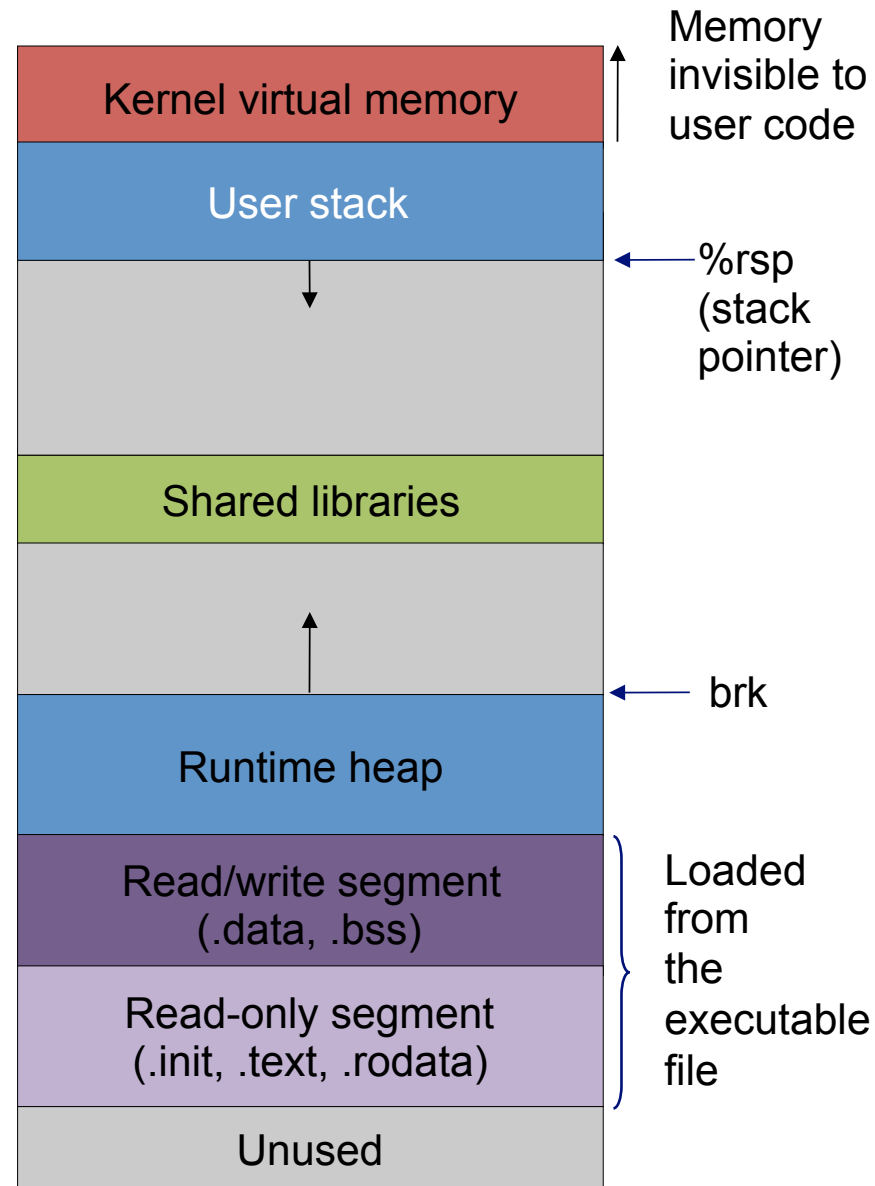
Do not know the size until the program runs (at runtime).

```
int main(void)
{
    int *array, i, n;

    scanf("%d", &n);
    array = (int *)malloc(n * sizeof(int));
    for (i = 0; i < n; i++)
        scanf("%d", &array[i]);
    exit(0);
}
```

Dynamic allocation on heap

Question: Is it possible to dynamically allocate memory on stack?



Dynamic allocation on heap

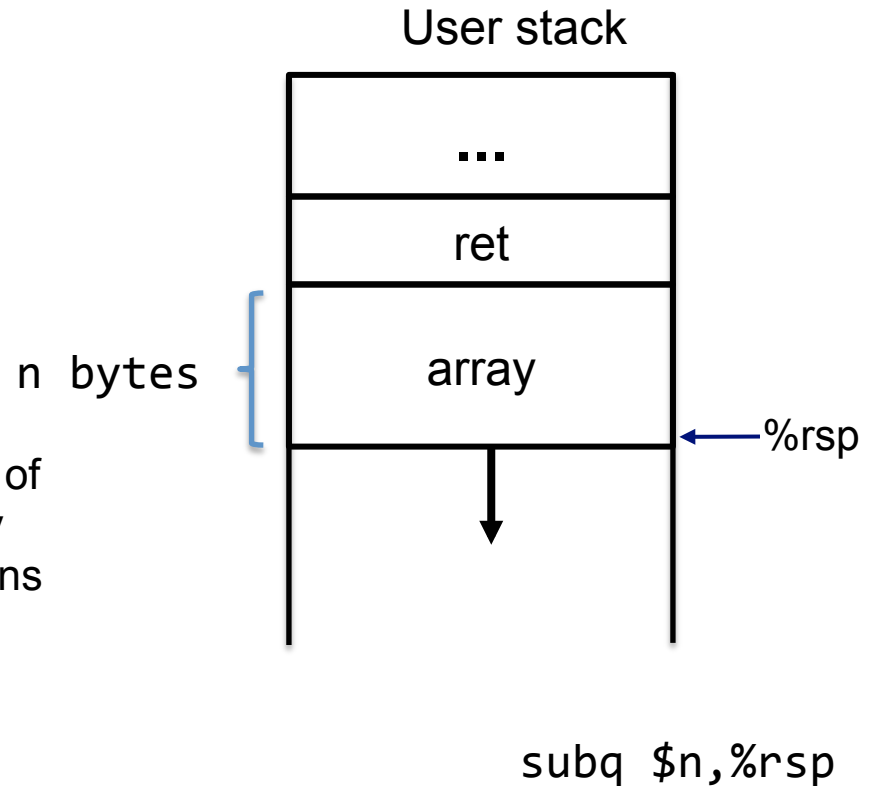
Question: Is it possible to dynamically allocate memory on stack?

Answer: Yes

```
void *alloca(size_t size);
```

Allocates size bytes of space in the stack frame of the caller. This temporary space is automatically freed when the function that called alloca() returns to its caller.

```
void func(int n) {  
    array = alloca(n);  
}
```



Dynamic allocation on heap

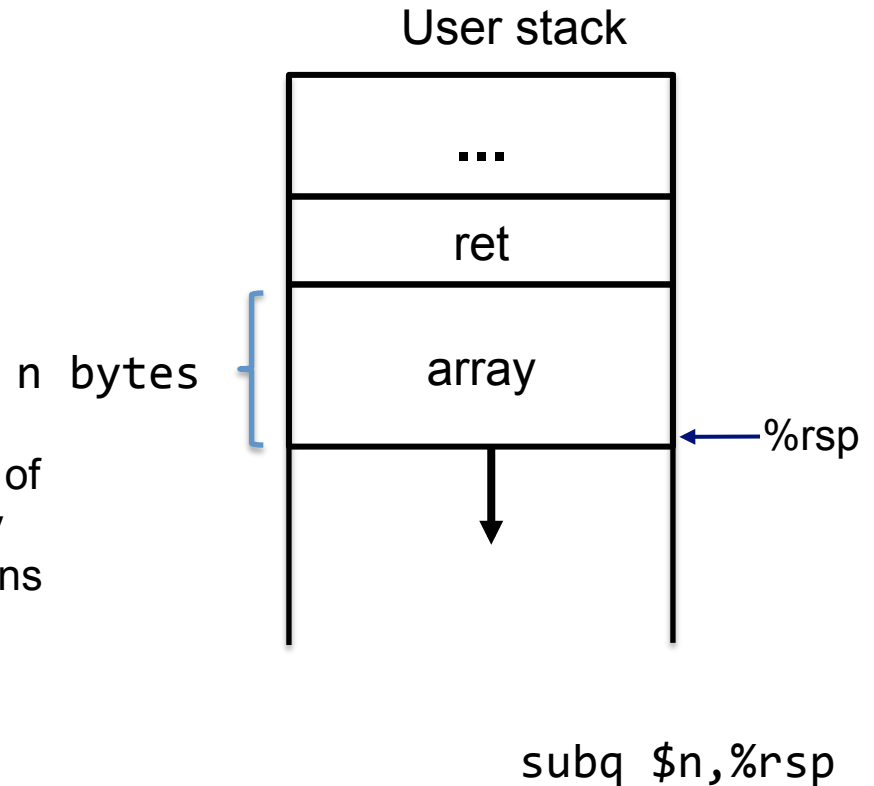
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```
void func(int n) {  
    array = alloca(n);  
}
```



Not good practice!

Dynamic allocation on heap

Question: Is it possible to dynamically allocate memory on stack?

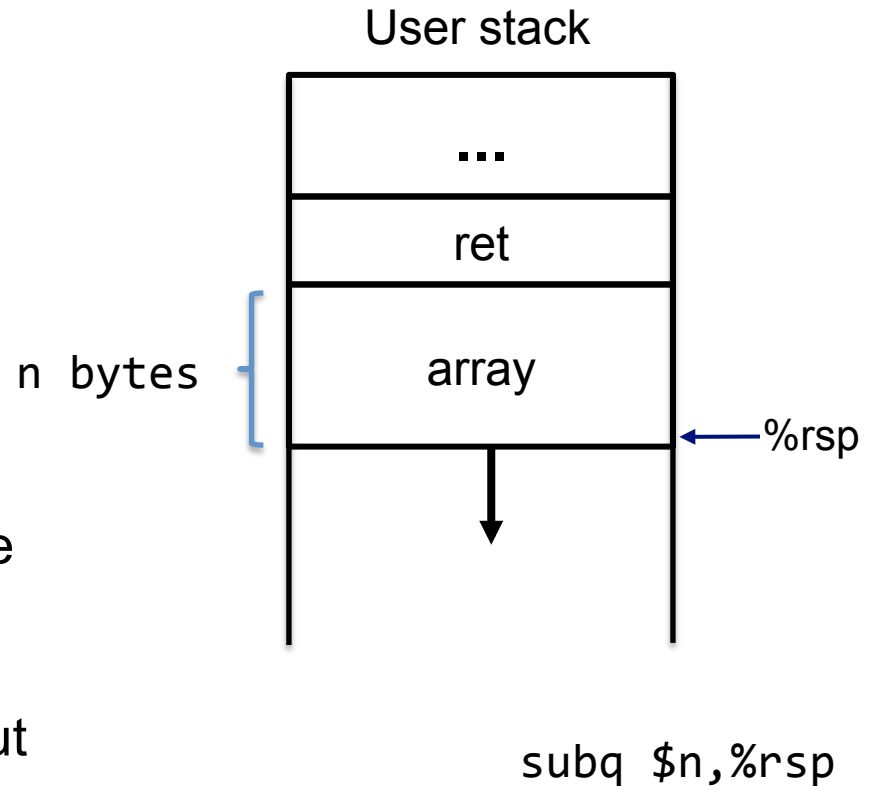
Answer: Yes

```
void *alloca(size_t size);
```

Issue I – Can not free memory until current function returns → Blowing the stack up

Issue II – Can not pass the memory out of the scope → Copy memories across different functions

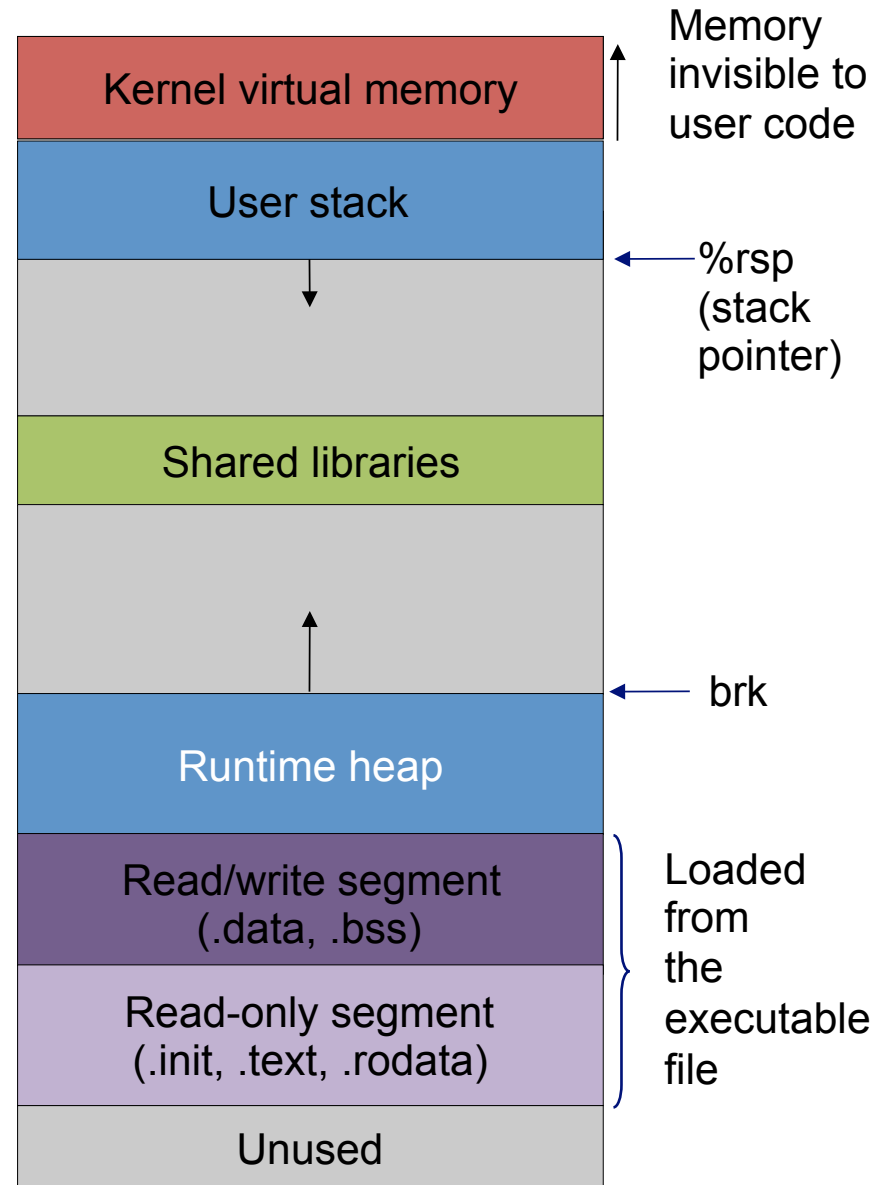
Issue III – Return value points to the top of the stack → buffer overflow (attack)



Not good practice!

Dynamic allocation on heap

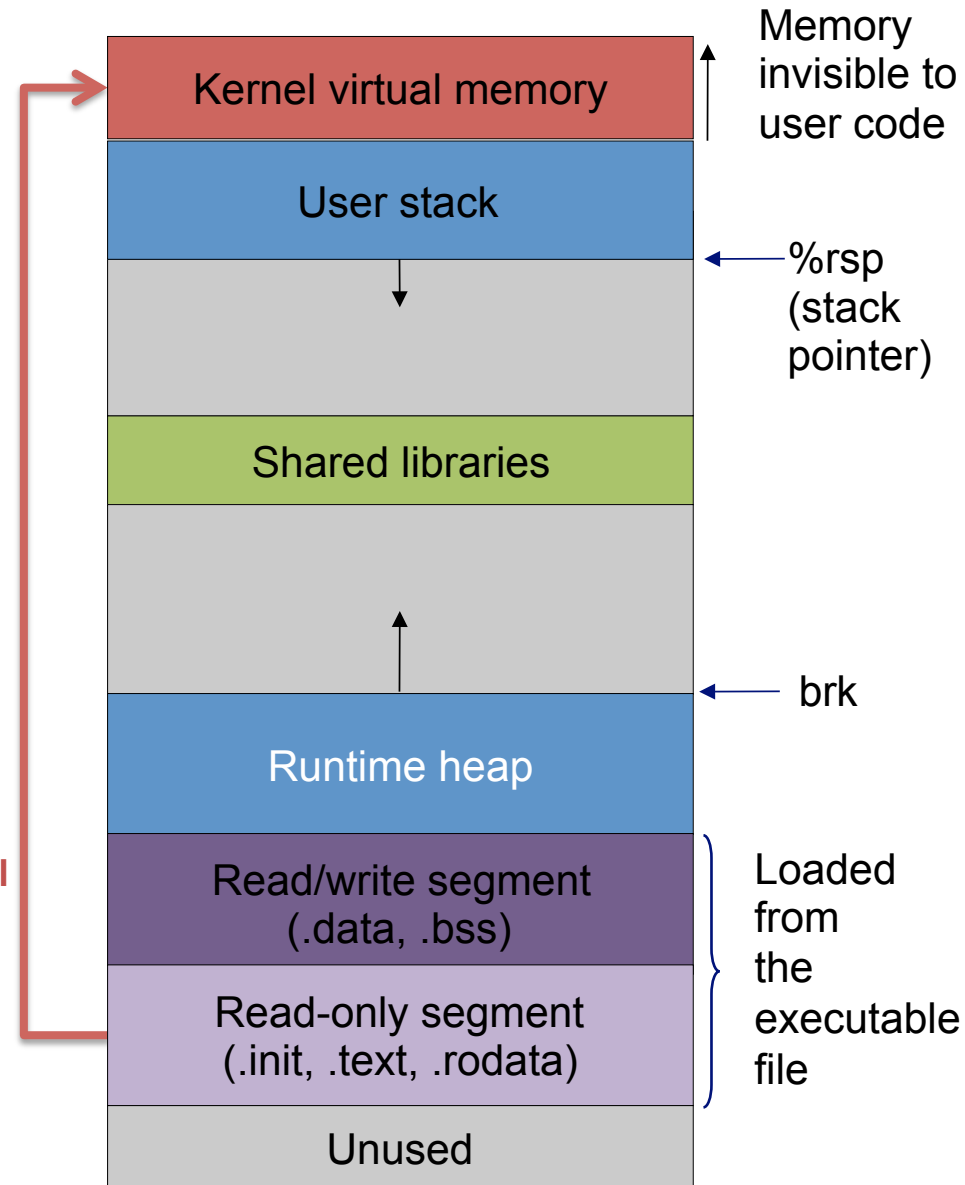
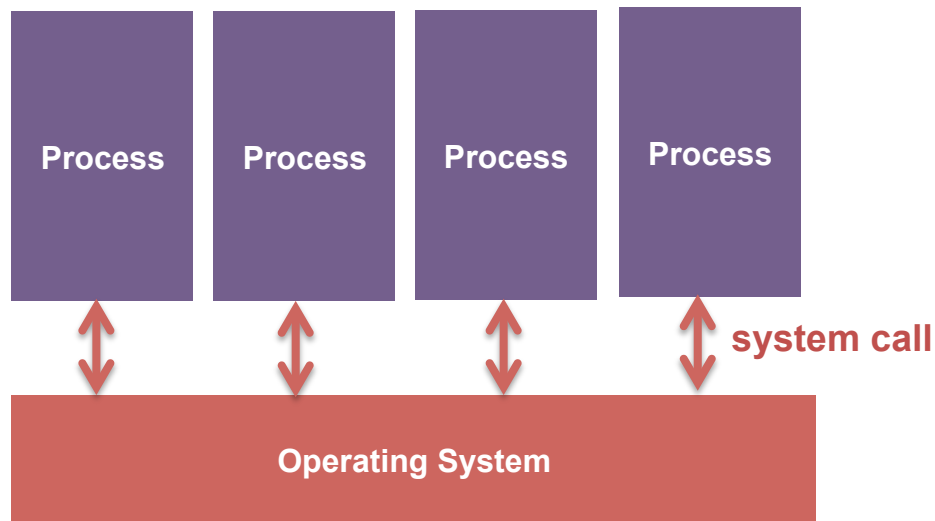
Question: How to allocate memory on heap?



Dynamic allocation on heap

Question: How to allocate memory on heap?

OS is responsible for heap.



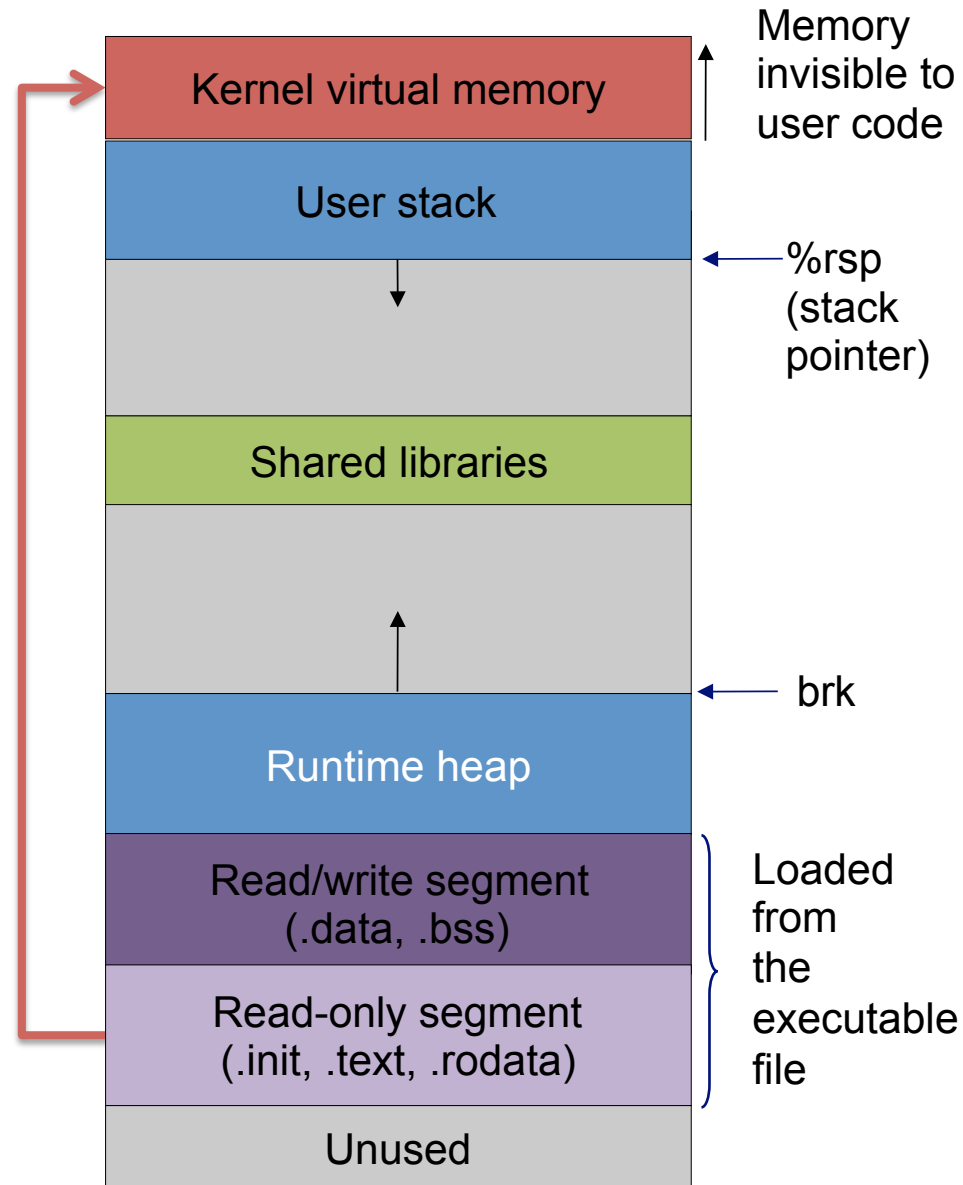
Dynamic allocation on heap

Question: How to allocate memory on heap?

OS is responsible for heap
– System calls

`void *sbrk(intptr_t size);` **sbrk**

It increases the top of heap by “size” and returns a pointer to the base of new storage. The “size” can be a negative number.



Dynamic allocation on heap

Question: How to allocate memory on heap?

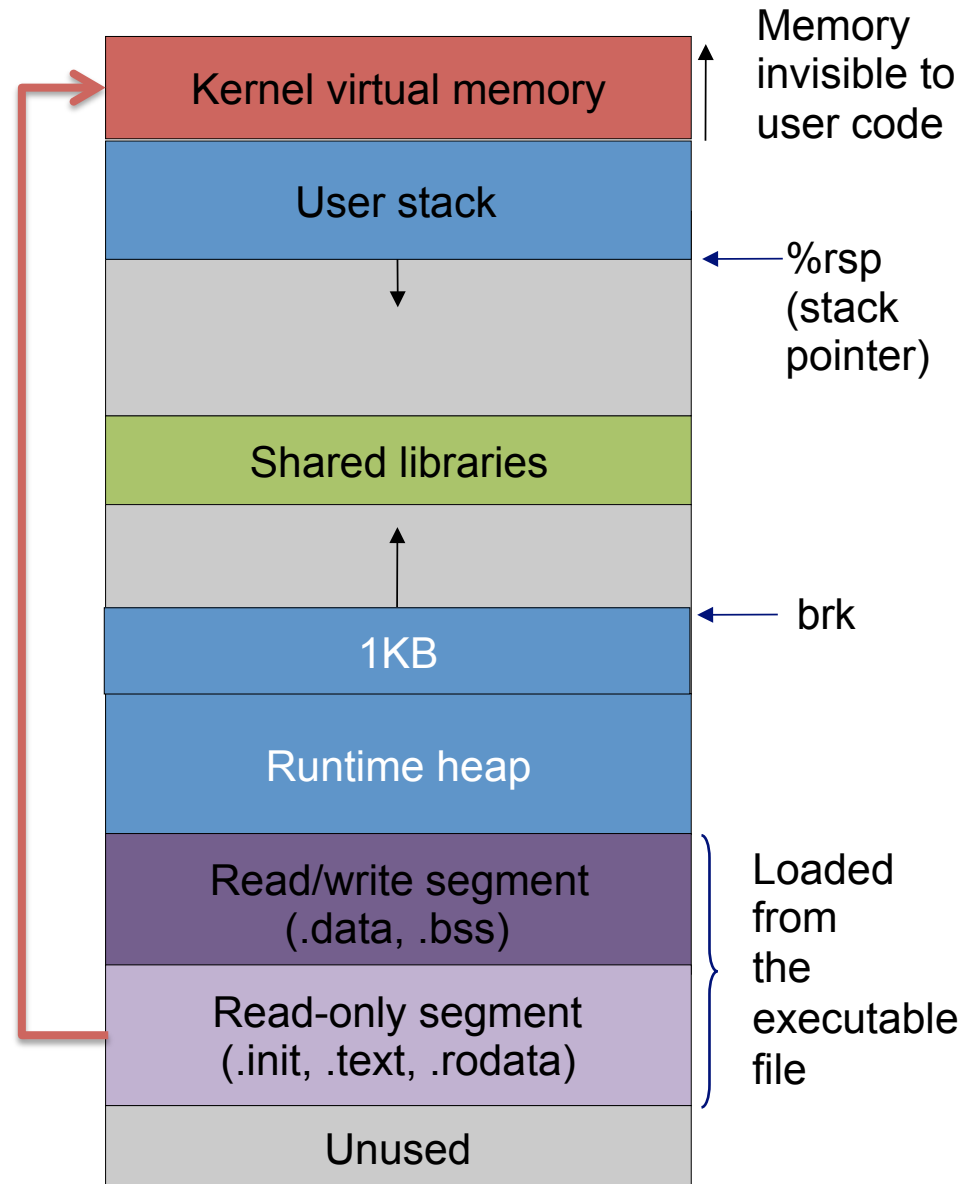
OS is responsible for heap
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```
void *sbrk(intptr_t size);
```

sbrk

It increases the top of heap by “size” and returns a pointer to the base of new storage. The “size” can be a negative number.

```
p = sbrk(1024) //allocate 1KB
```



Dynamic allocation on heap

Question: How to allocate memory on heap?

OS is responsible for heap
– System calls

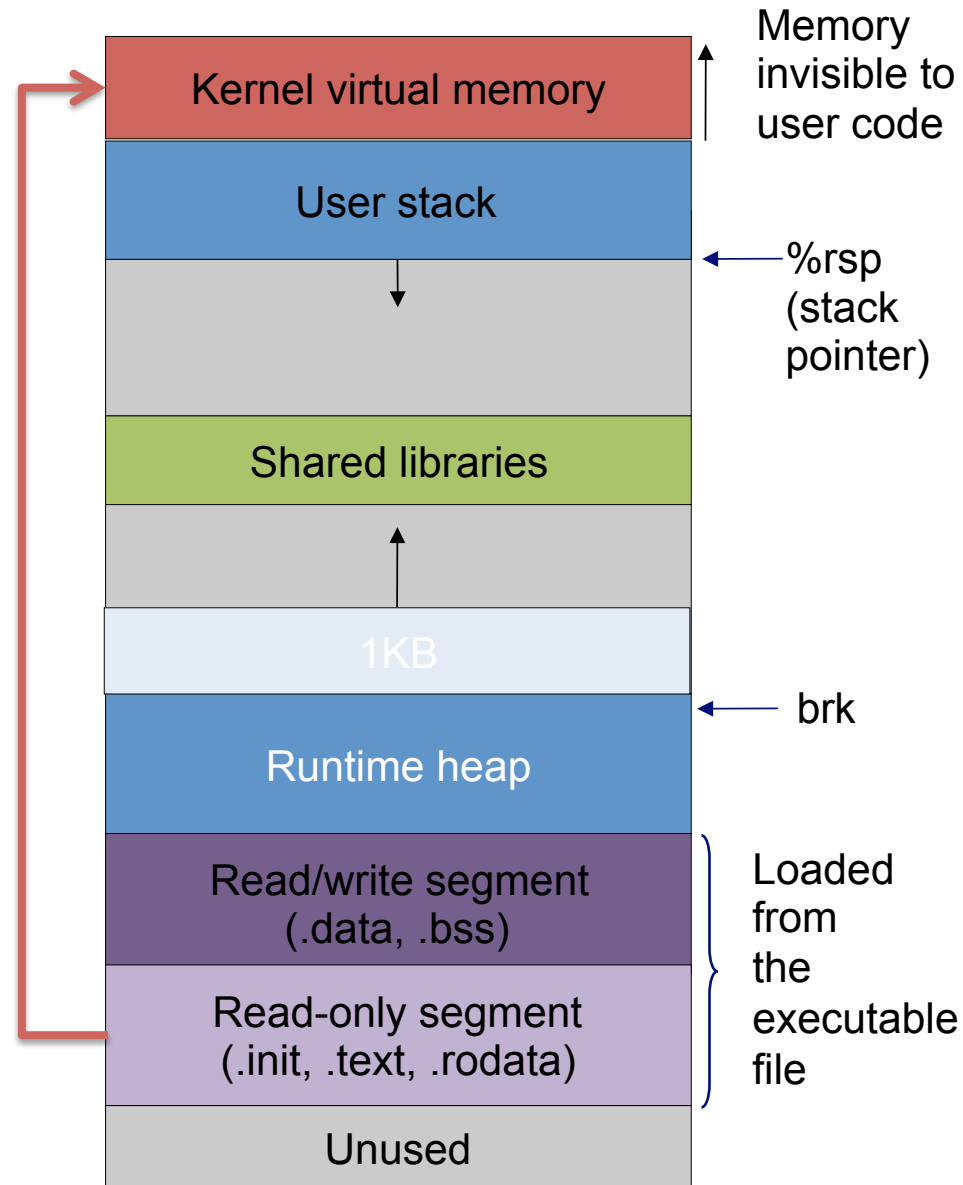
```
void *sbrk(intptr_t size);
```

sbrk

It increases the top of heap by “size” and returns a pointer to the base of new storage. The “size” can be a negative number.

```
p = sbrk(1024) //allocate 1KB
```

```
sbrk(-1024) //free p
```



Dynamic allocation on heap

Question: How to allocate memory on heap?

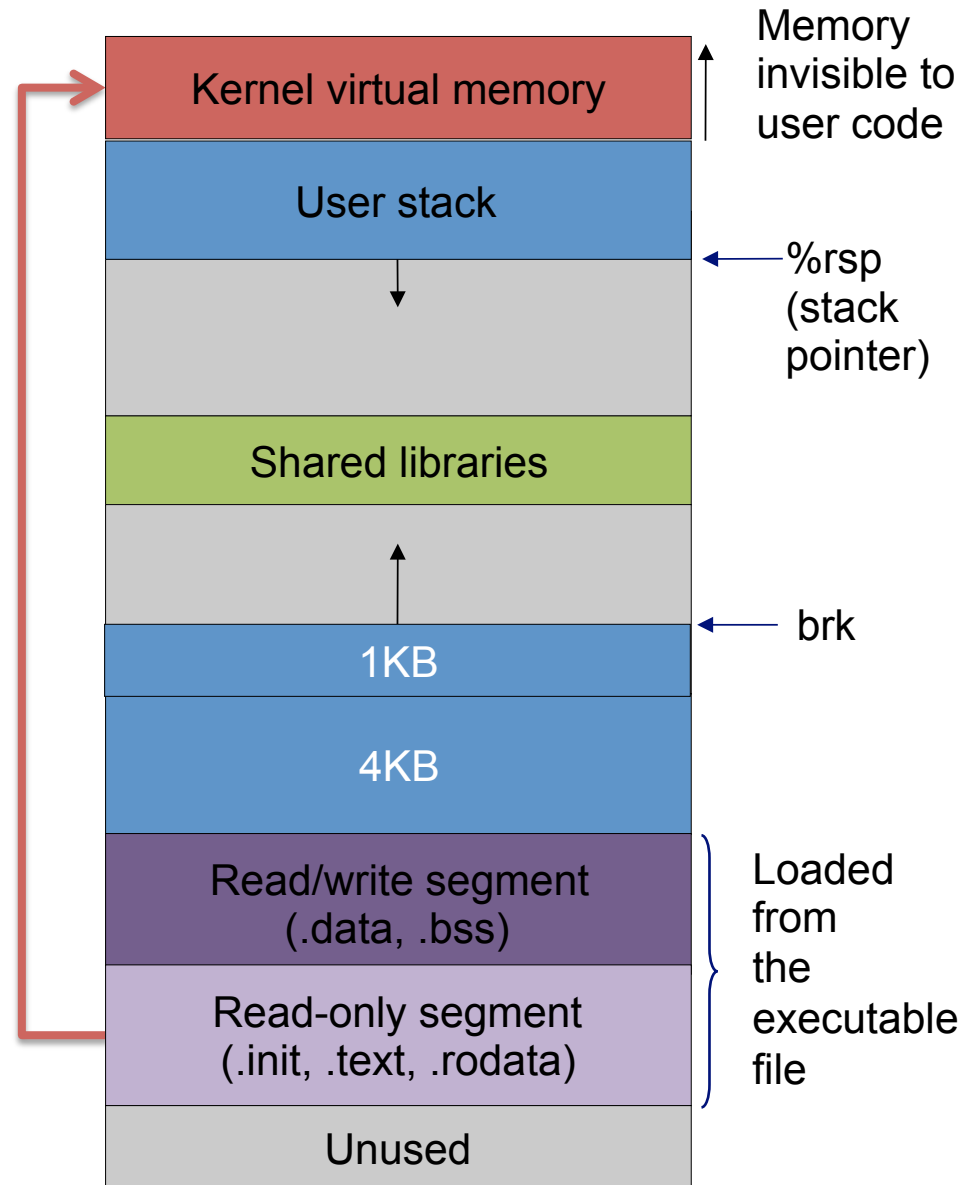
OS is responsible for heap
– System calls

`void *sbrk(intptr_t size);` *sbrk*

Issue I – can only free the memory on the top of heap

```
p1 = sbrk(1024) //allocate 1KB
p2 = sbrk(2048) //allocate 4KB
```

How to free p1?



Dynamic allocation on heap

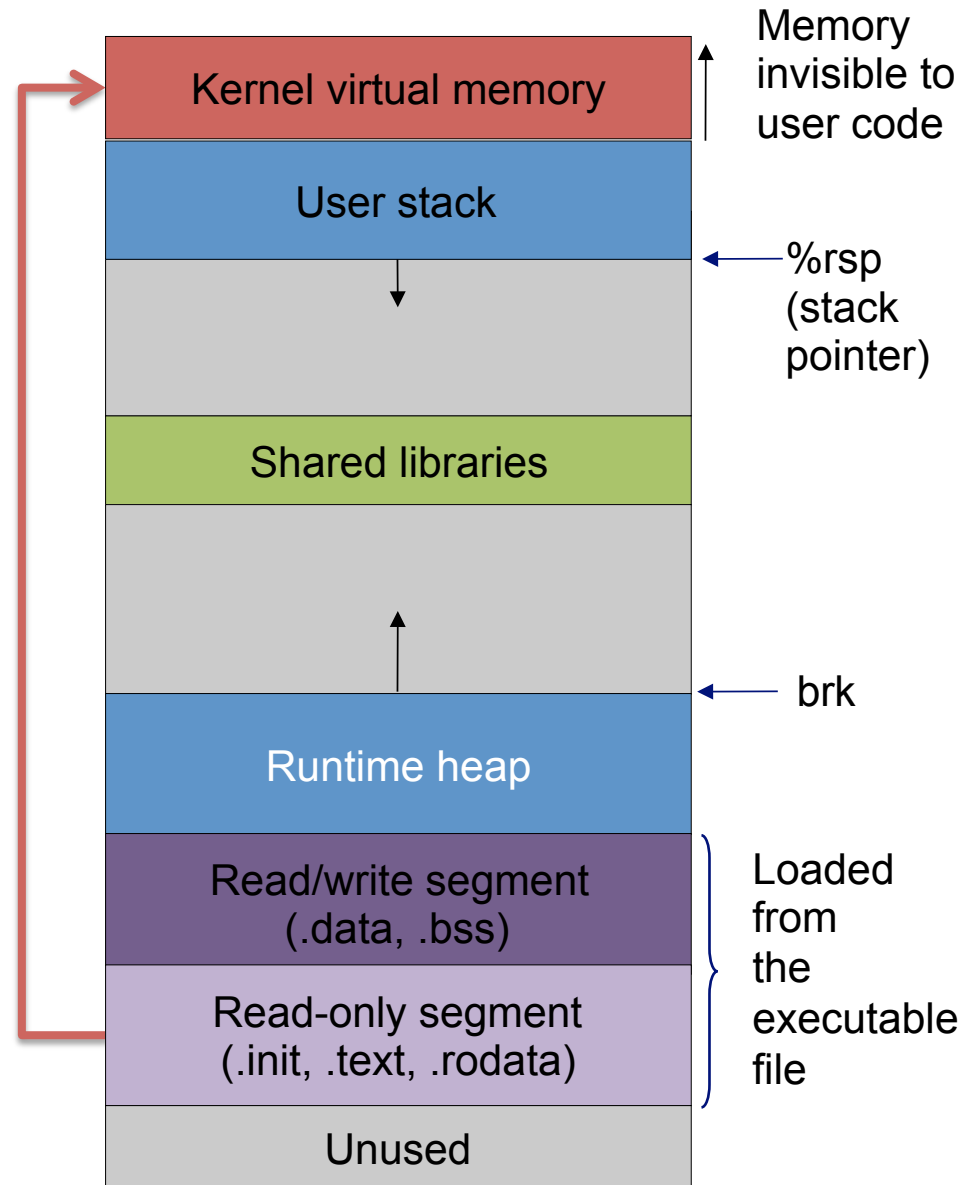
Question: How to allocate memory on heap?

OS is responsible for heap
– System calls

`void *sbrk(intptr_t size);` `sbrk`

Issue I – can only free the memory on the top of heap

Issue II – system call has high performance cost > 10X

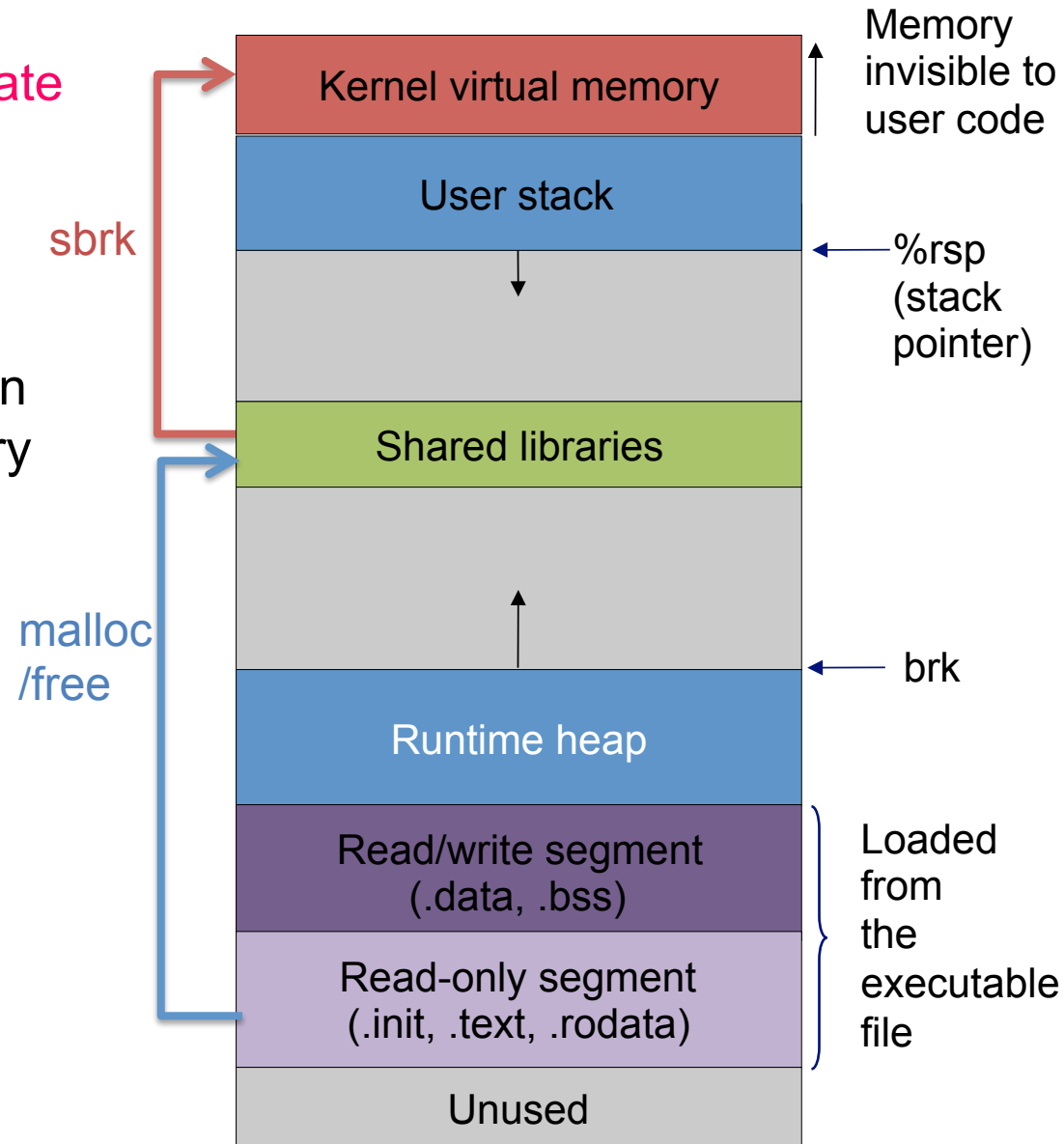


Dynamic allocation on heap

Question: How to efficiently allocate memory on heap?

Basic idea – request a large of memory region from heap once, then manage this memory region by itself. → allocator in the library

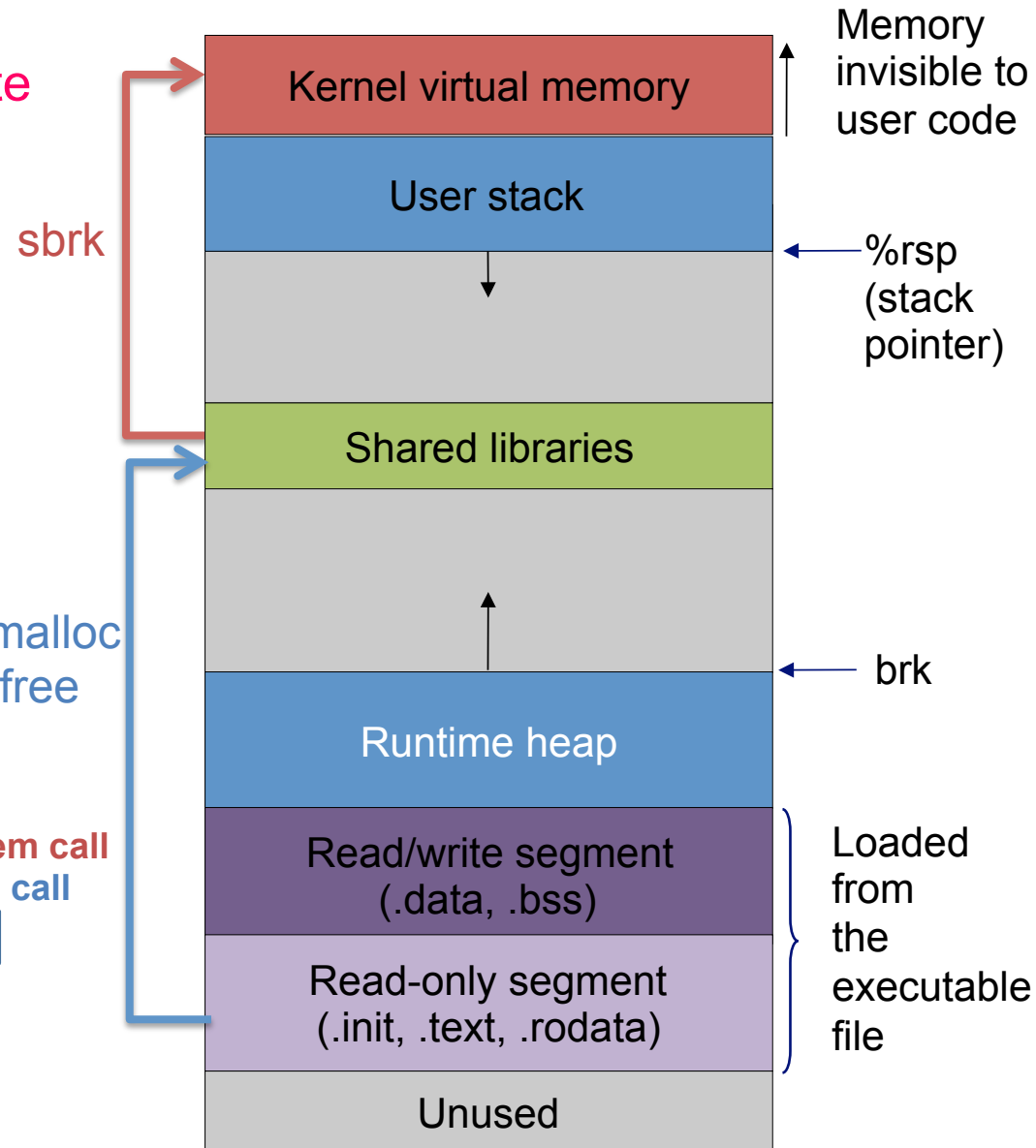
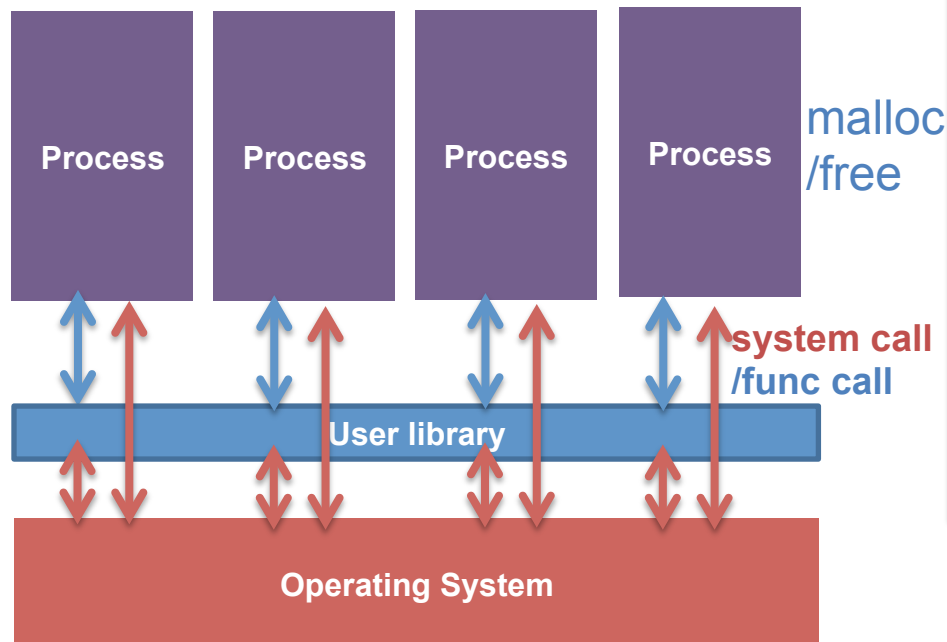
Memory management in the user space.



Dynamic allocation on heap

Question: How to efficiently allocate memory on heap?

Basic idea – request a large of memory region from heap once, then manage this memory region by itself. → allocator in the library



Memory Allocator

Assumption in this lecture

- At the beginning, the allocator requests enough memory with `sbrk`

Goal

- Highly utilize the acquired memory with high throughput
 - high throughput – how many mallocs / frees can be done per second
 - high utilization – fraction of allocated size / total heap size

Memory Allocator

Assumed behavior of applications

- Can issue arbitrary sequence of malloc (for arbitrary sizes)/free
- The argument of free must be the return value of a previous malloc
- No double free

Requirements of allocator

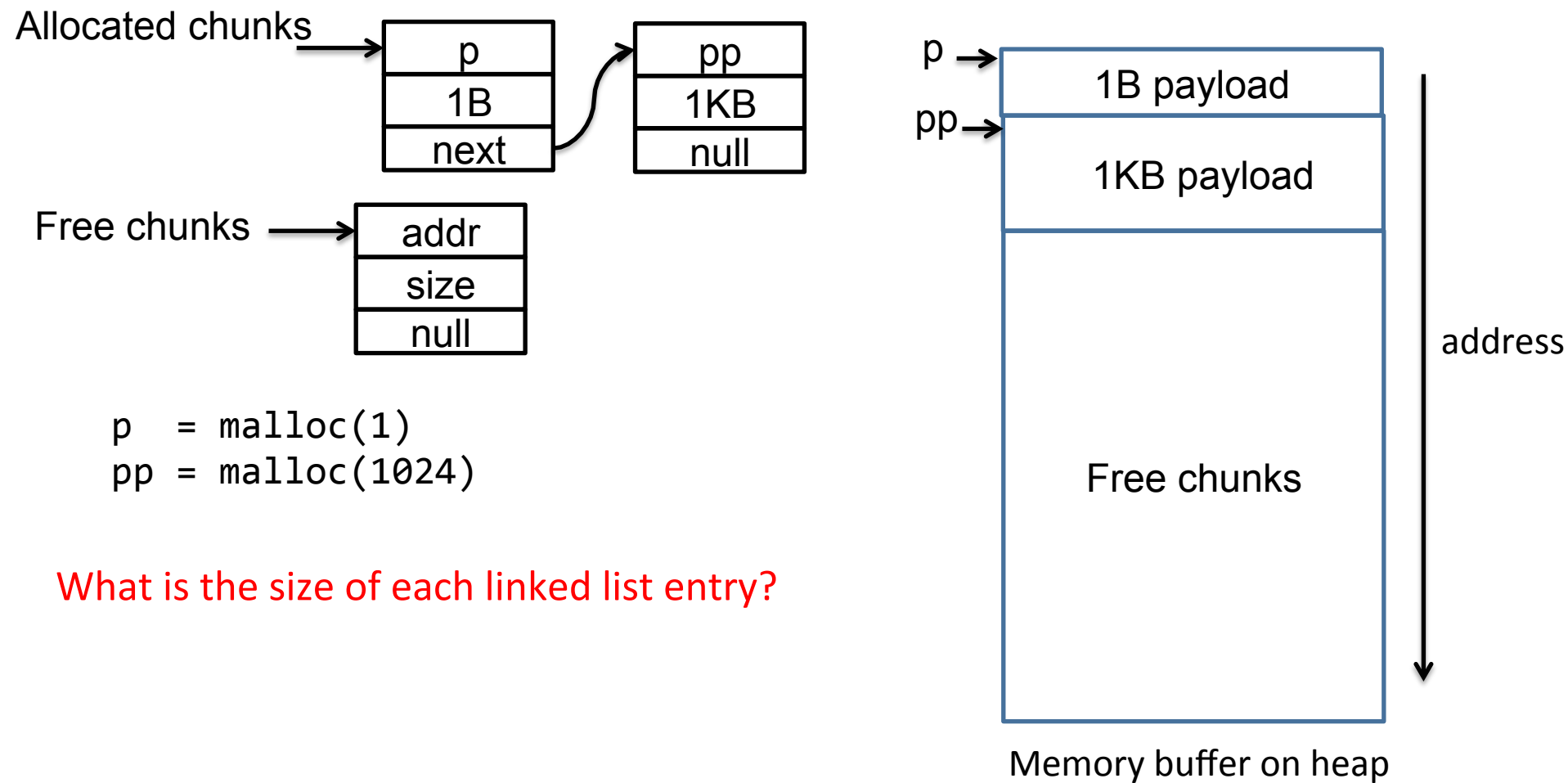
- Must allocate from free memory (correctness)
- Once allocated, cannot be moved

Questions

1. How to keep track which bytes are free and which are not?
2. Which of the free chunks to allocate?
3. free only supplies a pointer, how to know its corresponding chunk size?

Track allocated/free chunks

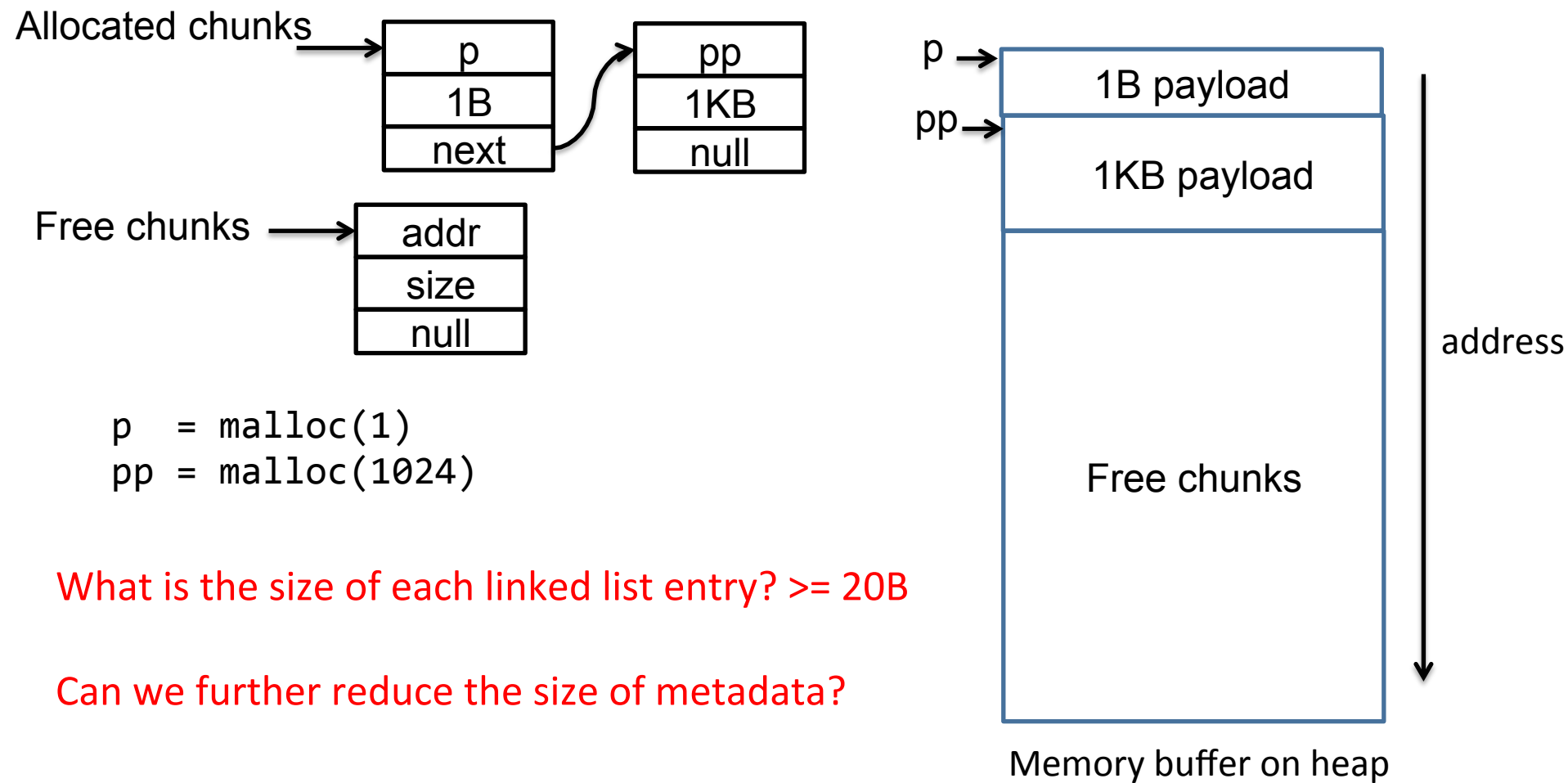
Keep the metadata (addr, size) in a linked list



What is the size of each linked list entry?

Track allocated/free chunks

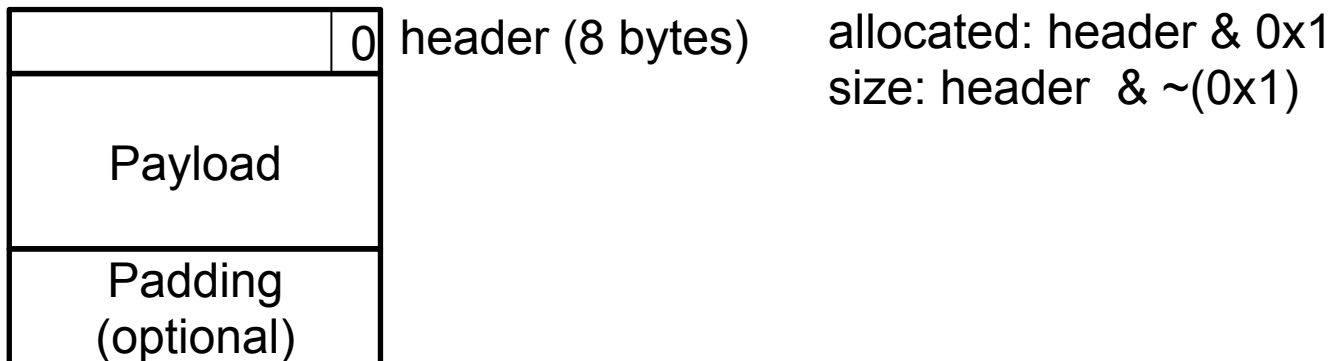
Keep the metadata (addr, size) in a linked list



Implicit list

Embed the metadata in the chunks (blocks)

- Each block has a one-word (8 bytes) header
- Block is double-word (16 bytes) alignment
 - Size is multiple of 16

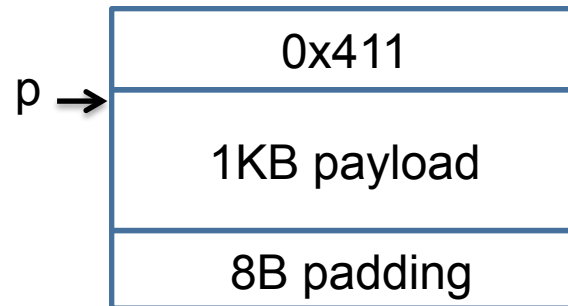


Implicit list

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```
p = malloc(1024)
```

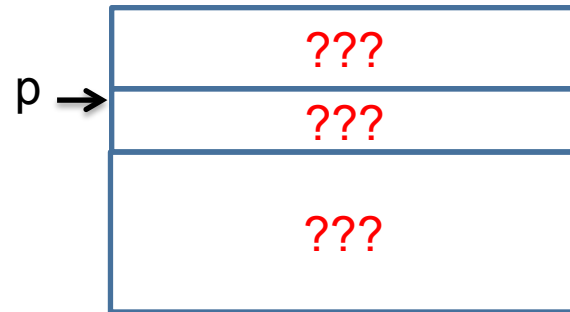


Implicit list

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p = malloc(1)
```

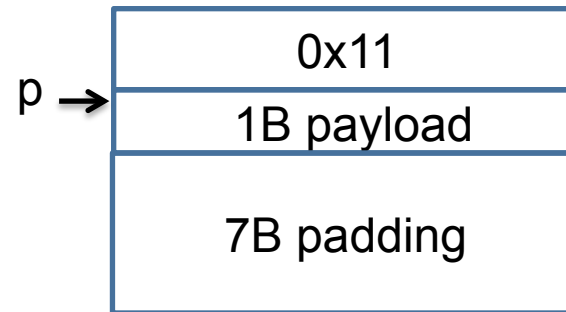


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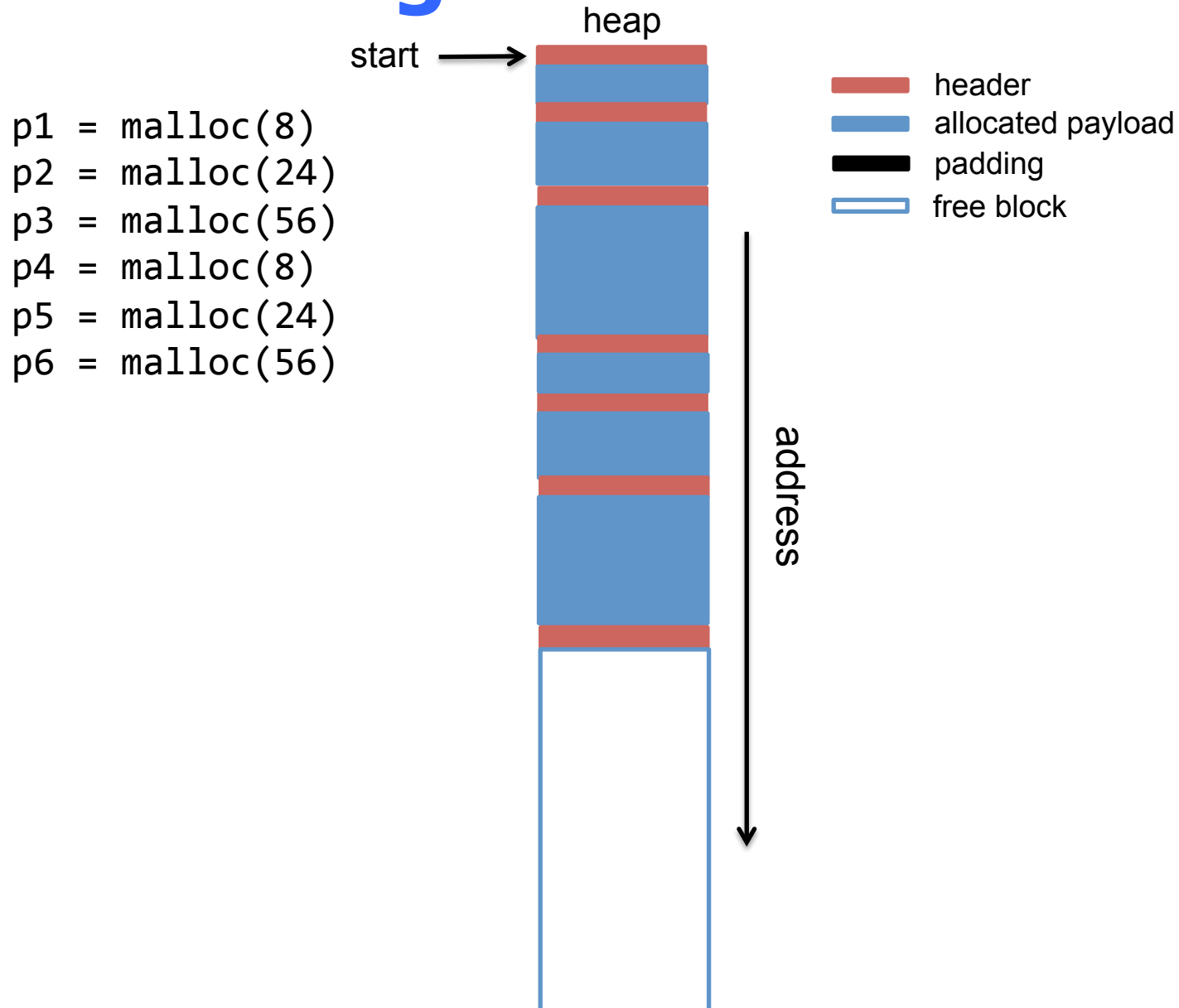
Exercises

| Alignment | Request | Block size | Header (hex) |
|-----------|------------|------------|--------------|
| 8 bytes | malloc(5) | | |
| 4 bytes | malloc(13) | | |
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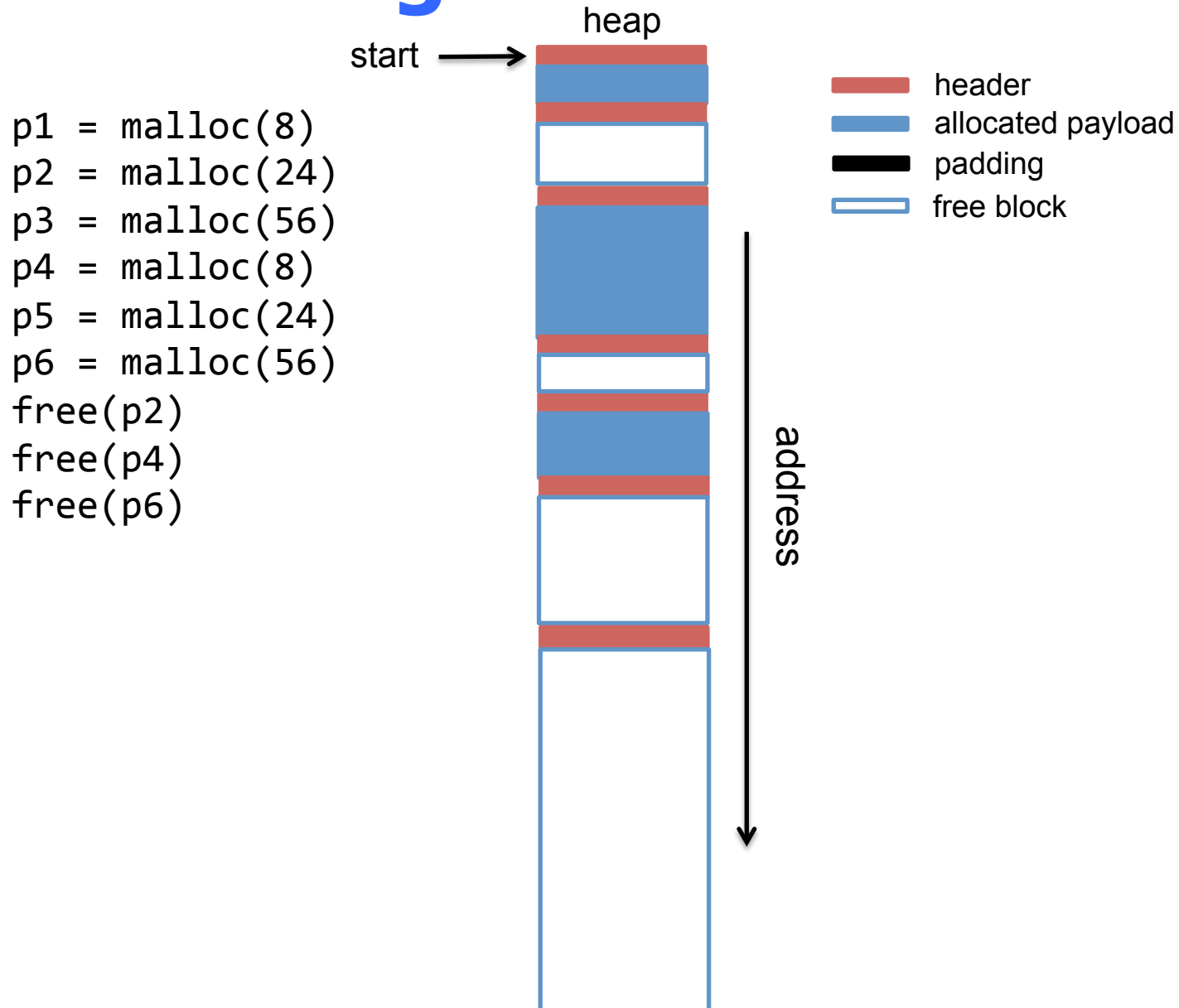
Exercises

| Alignment | Request | Block size | Header (hex) |
|-----------|------------|------------|--------------|
| 8 bytes | malloc(5) | 16 | 0x11 |
| 4 bytes | malloc(13) | 24 | 0x19 |
| 16 bytes | malloc(20) | 32 | 0x21 |
| 8 bytes | malloc(3) | 16 | 0x11 |

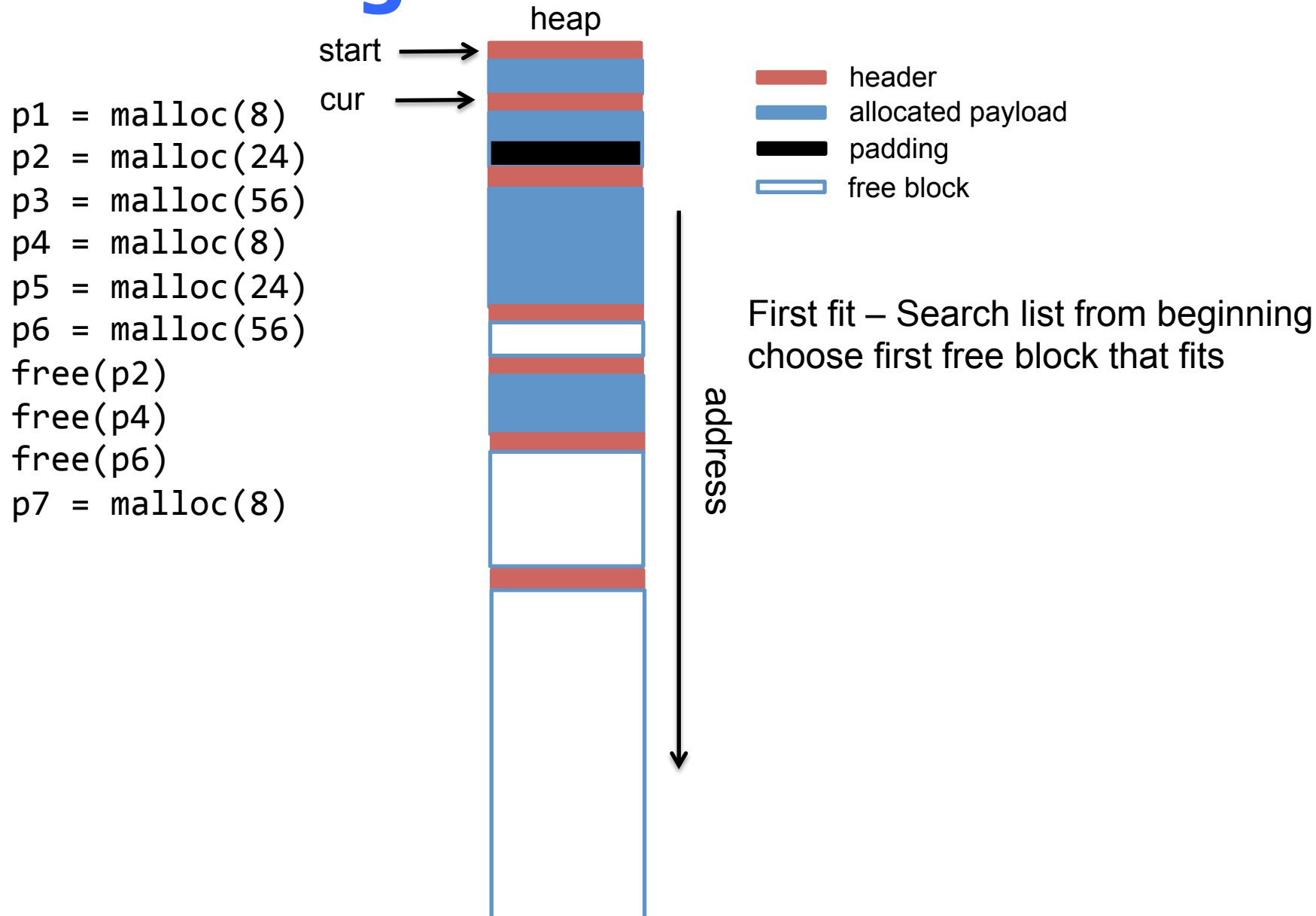
Placing allocated blocks



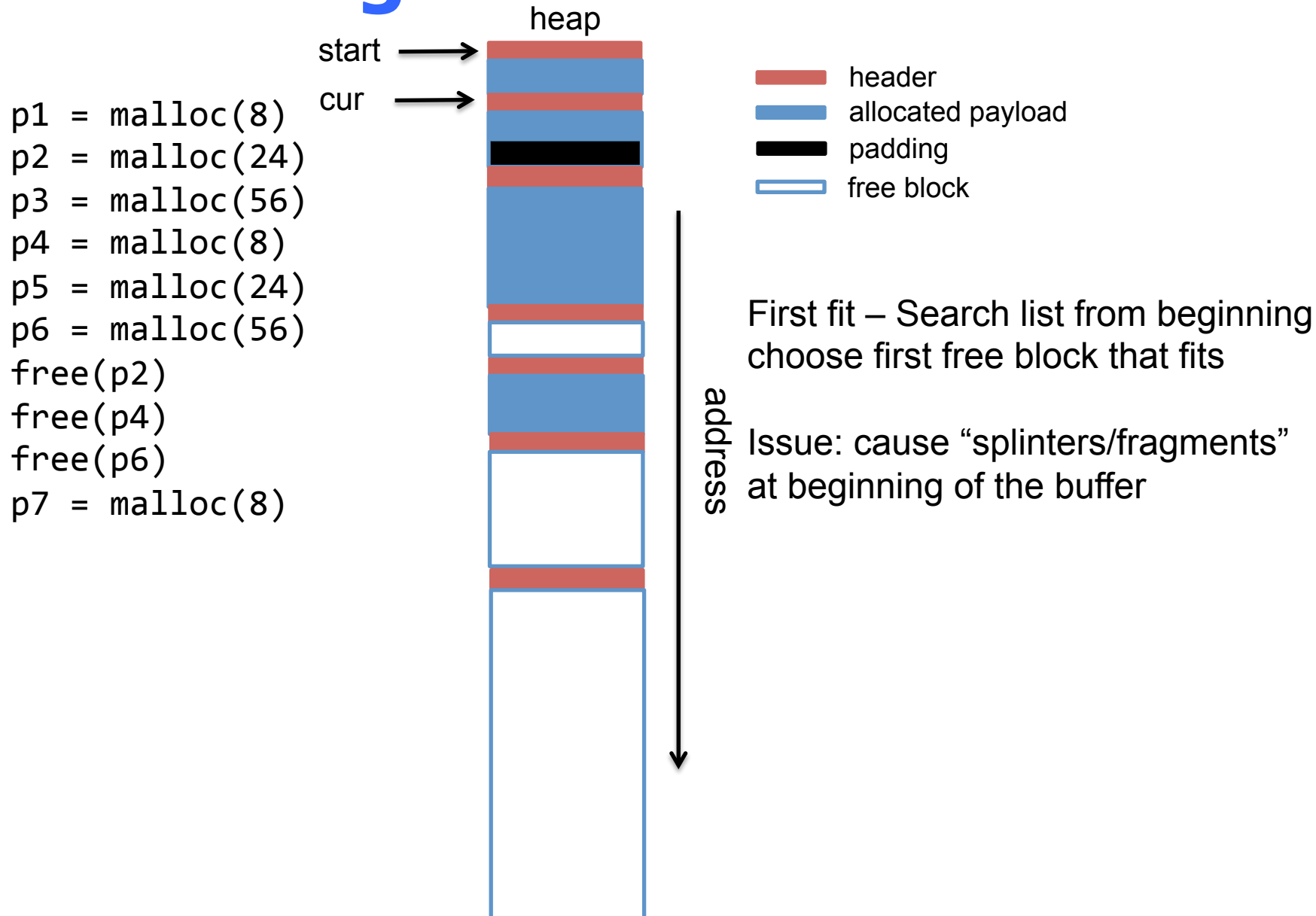
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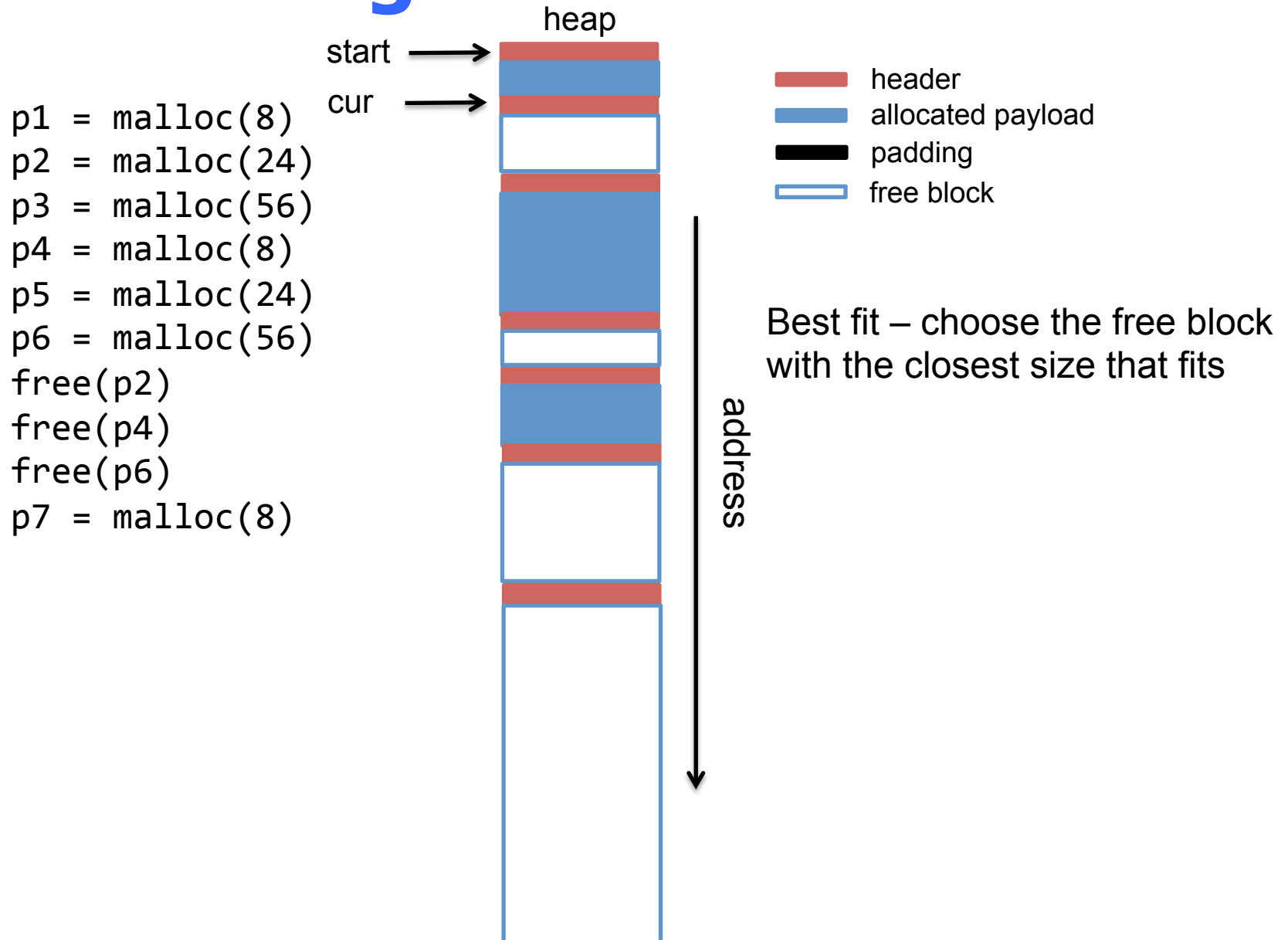
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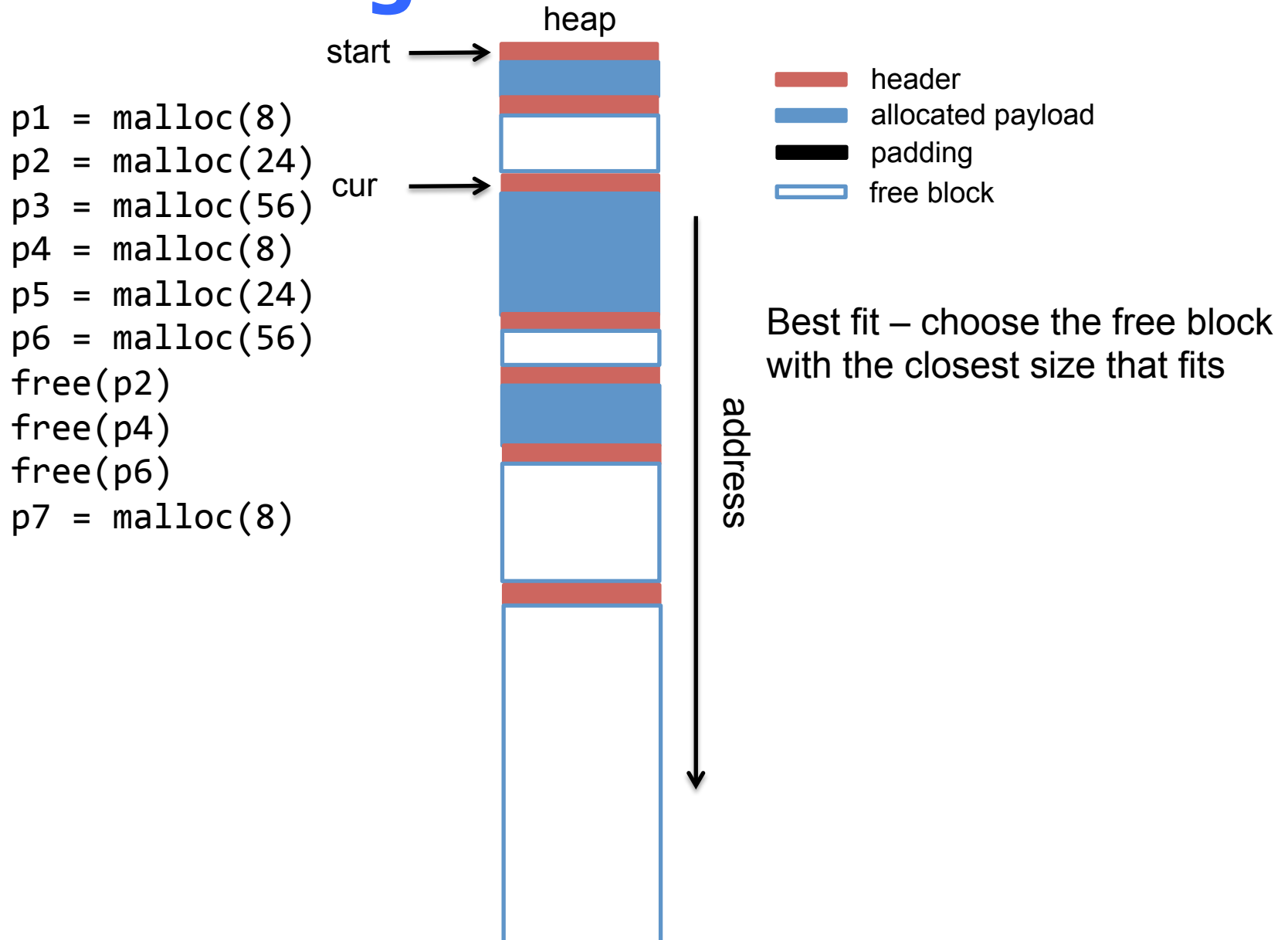
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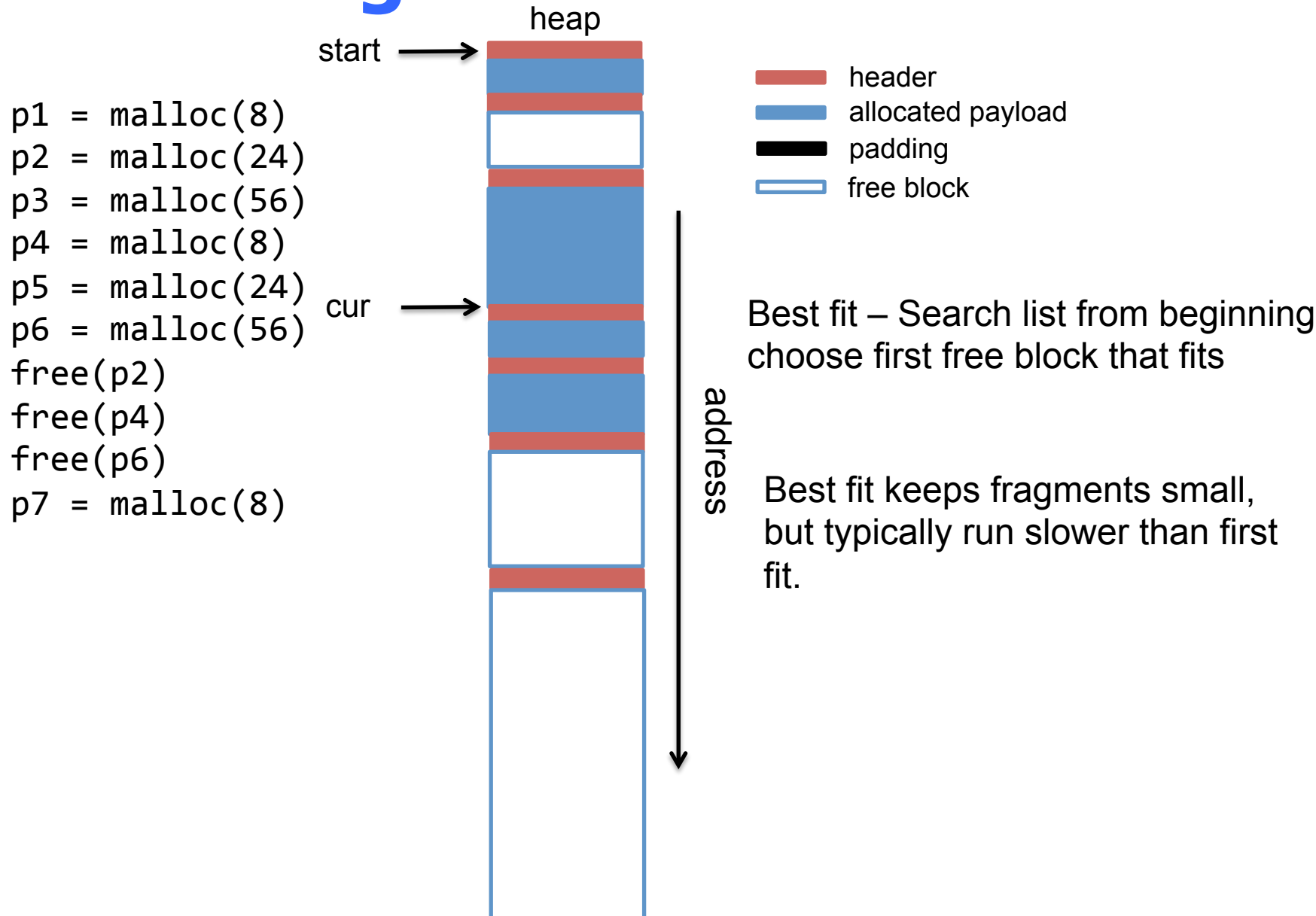
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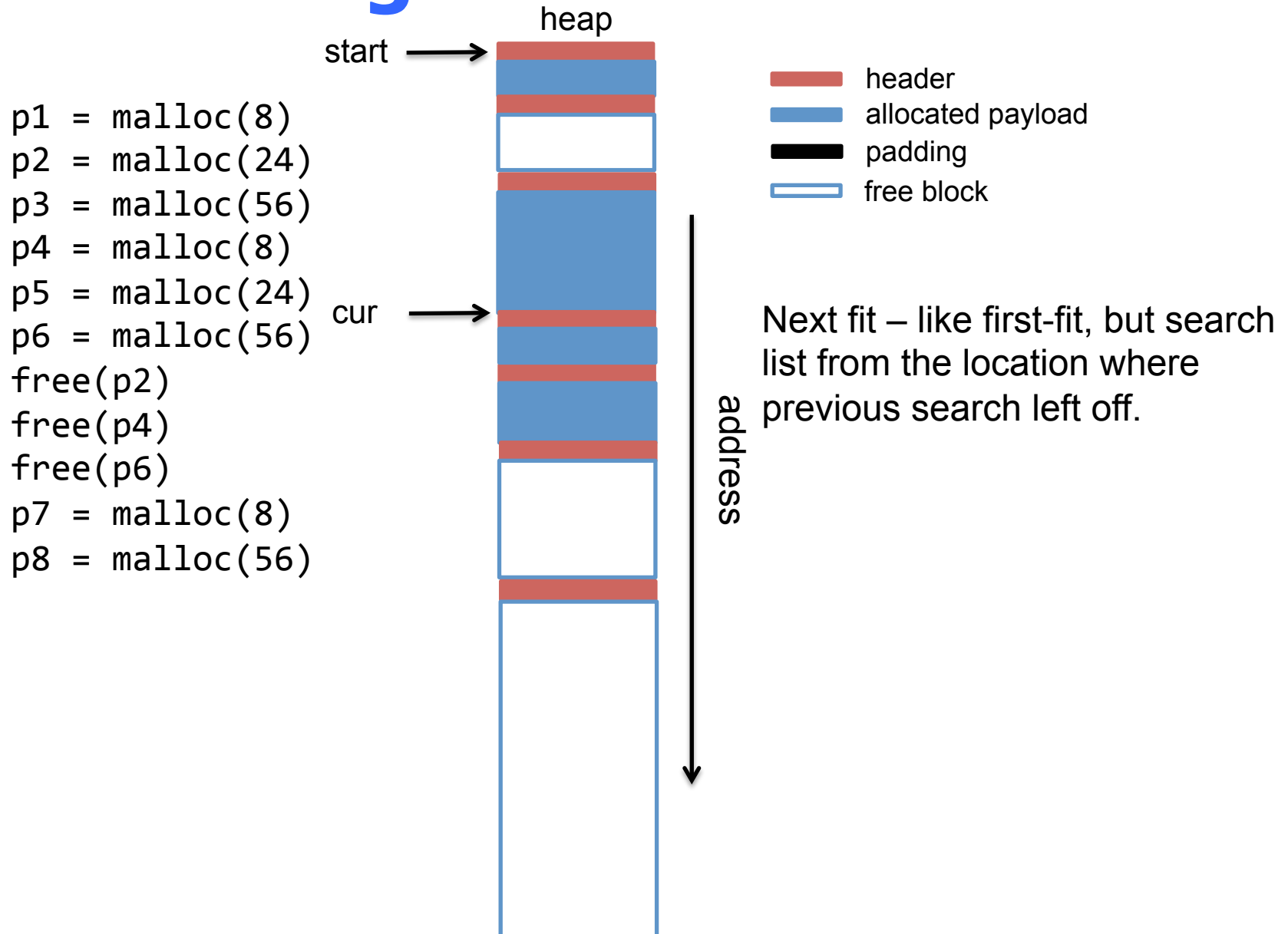
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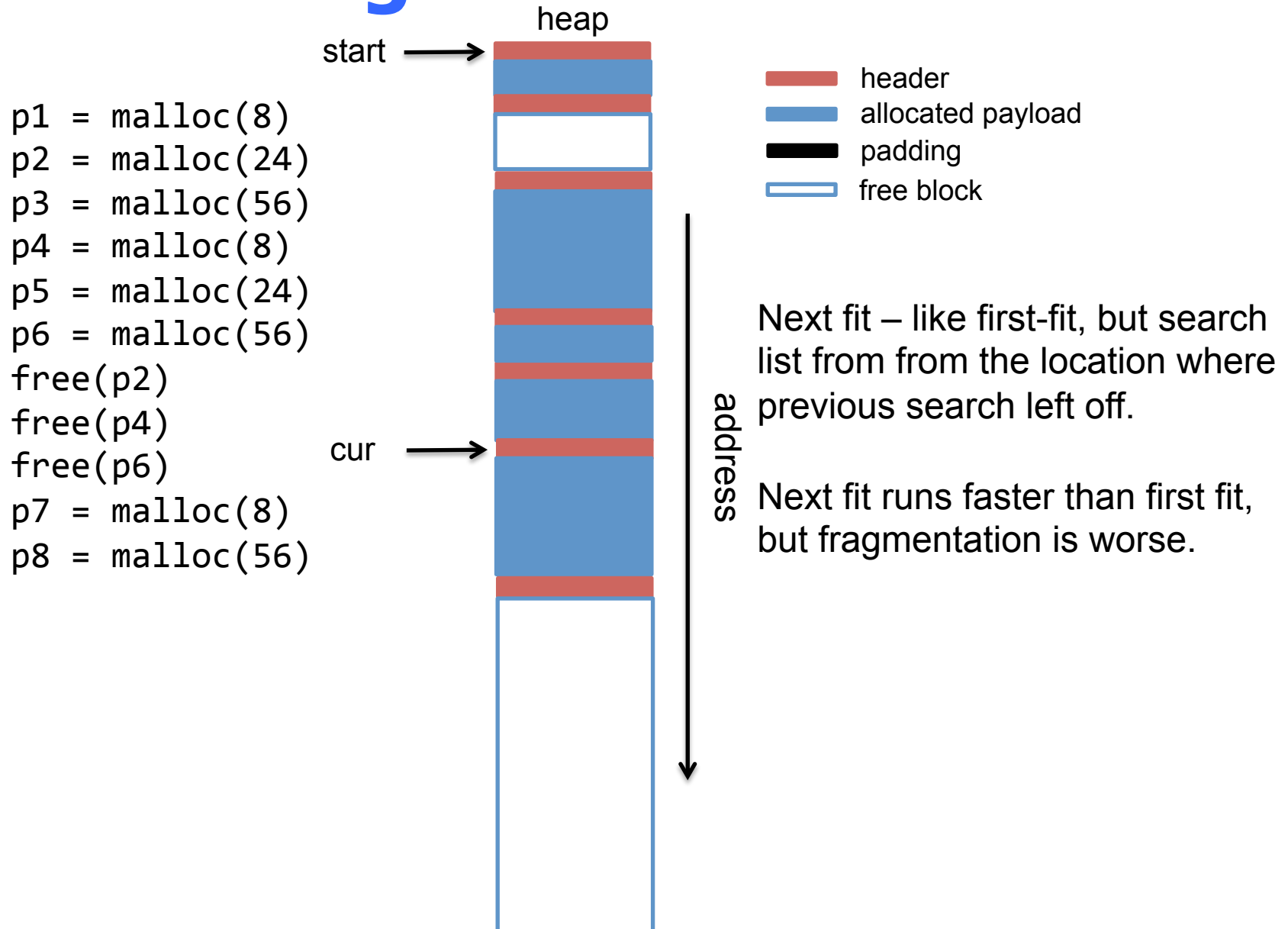
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Placing allocated blocks

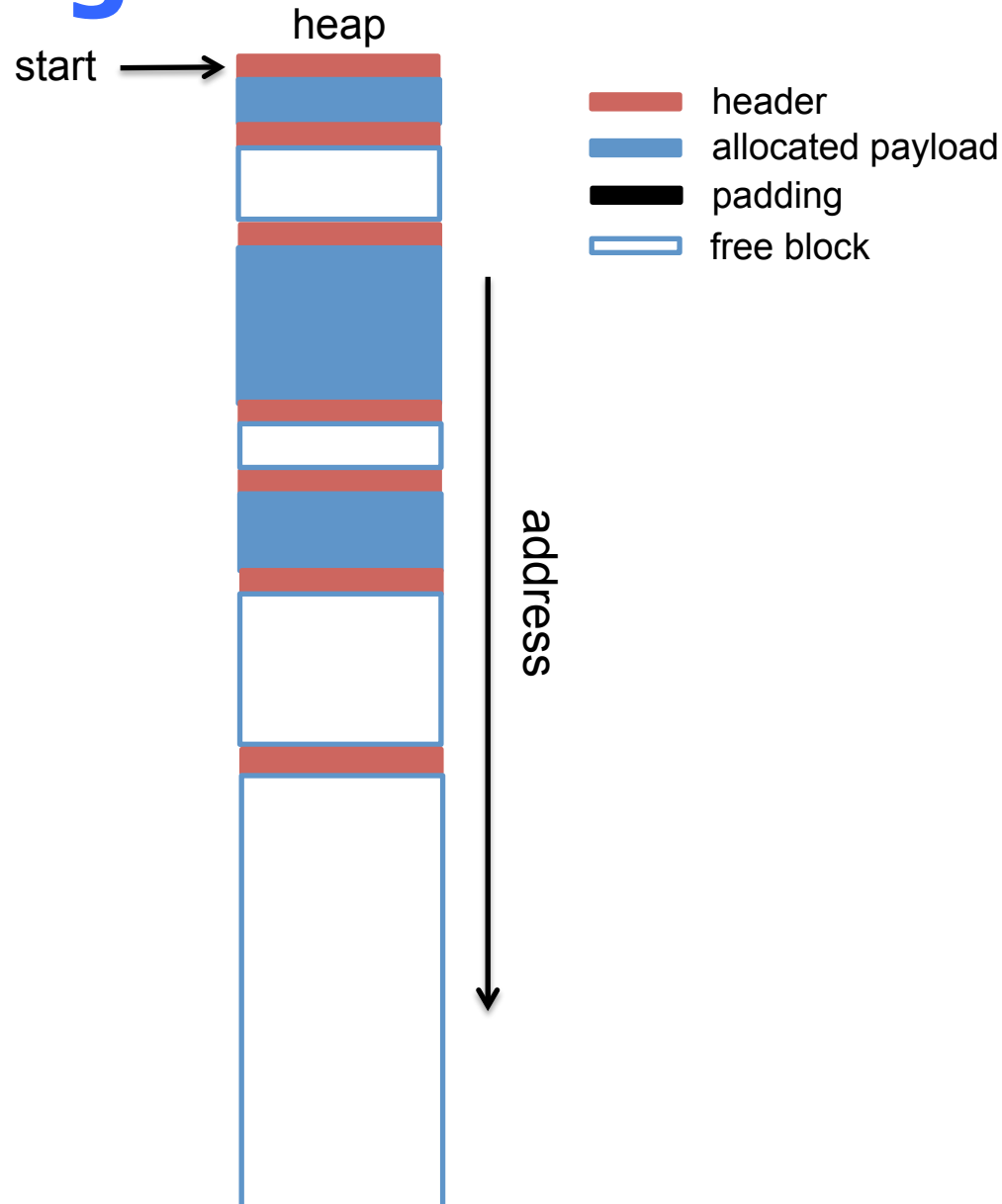


Placing allocated blocks



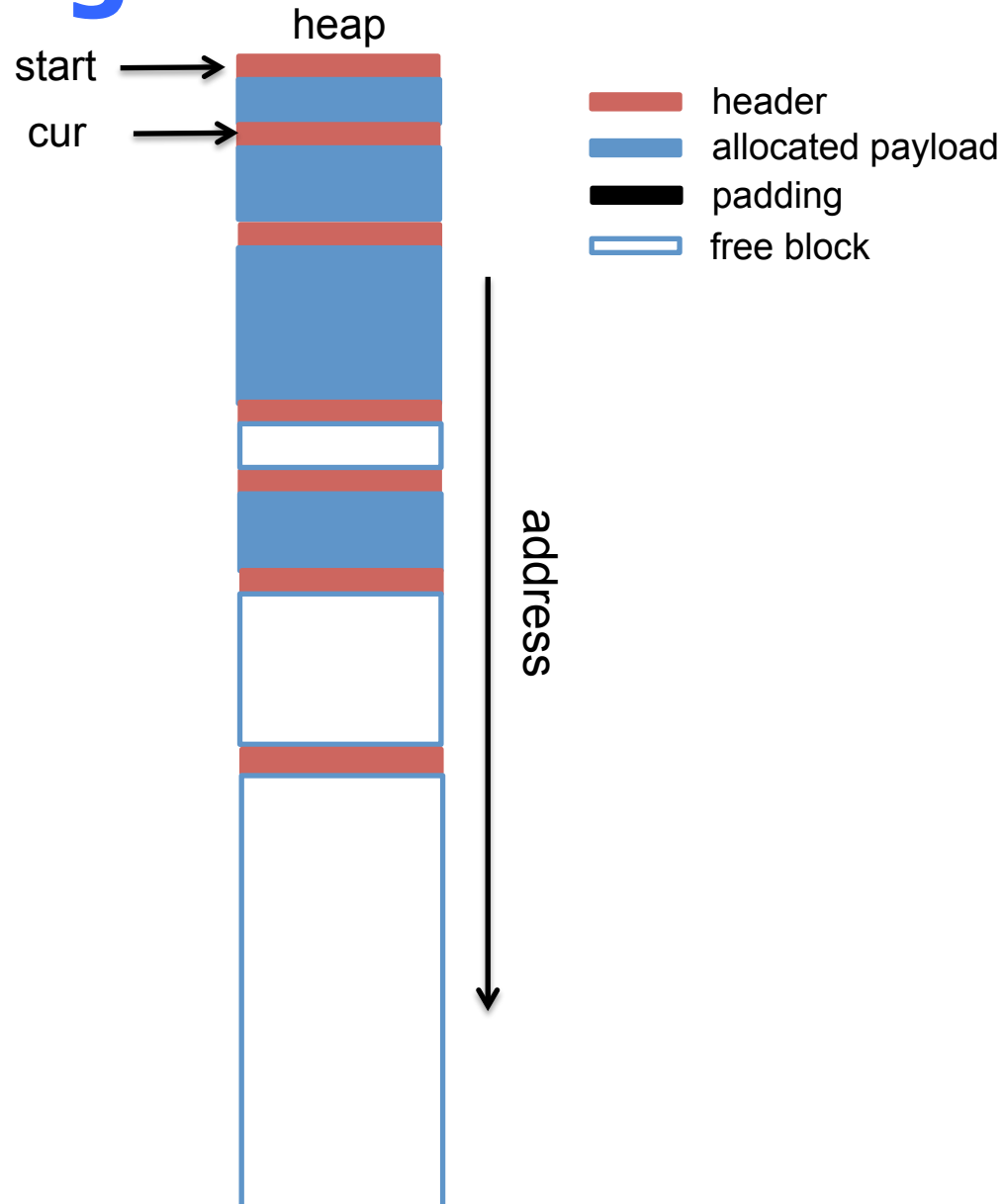
Placing allocated blocks

```
p1 = malloc(8)
p2 = malloc(24)
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free(p2)
free(p4)
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p7 = malloc(24)
p8 = malloc(24)
```



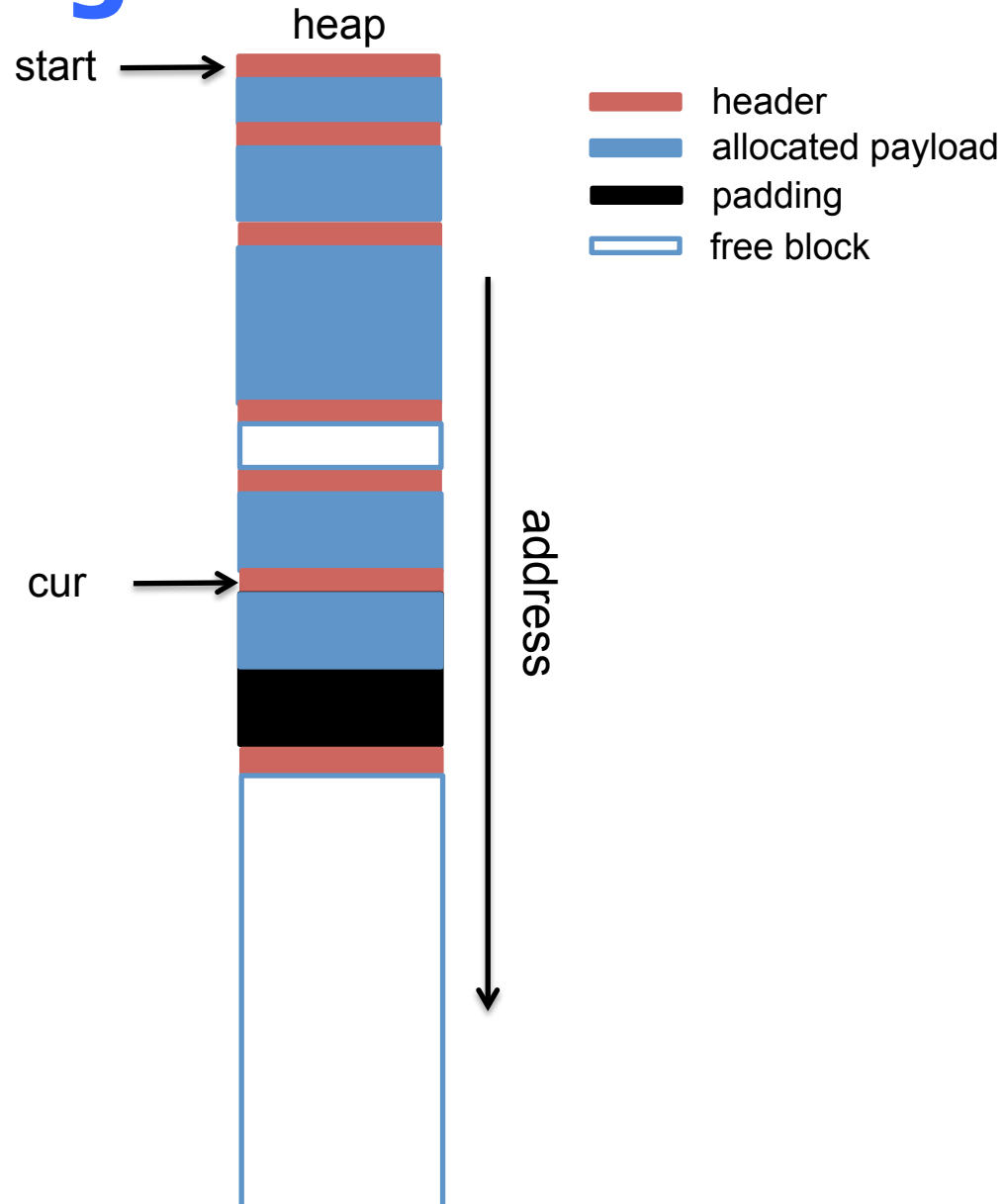
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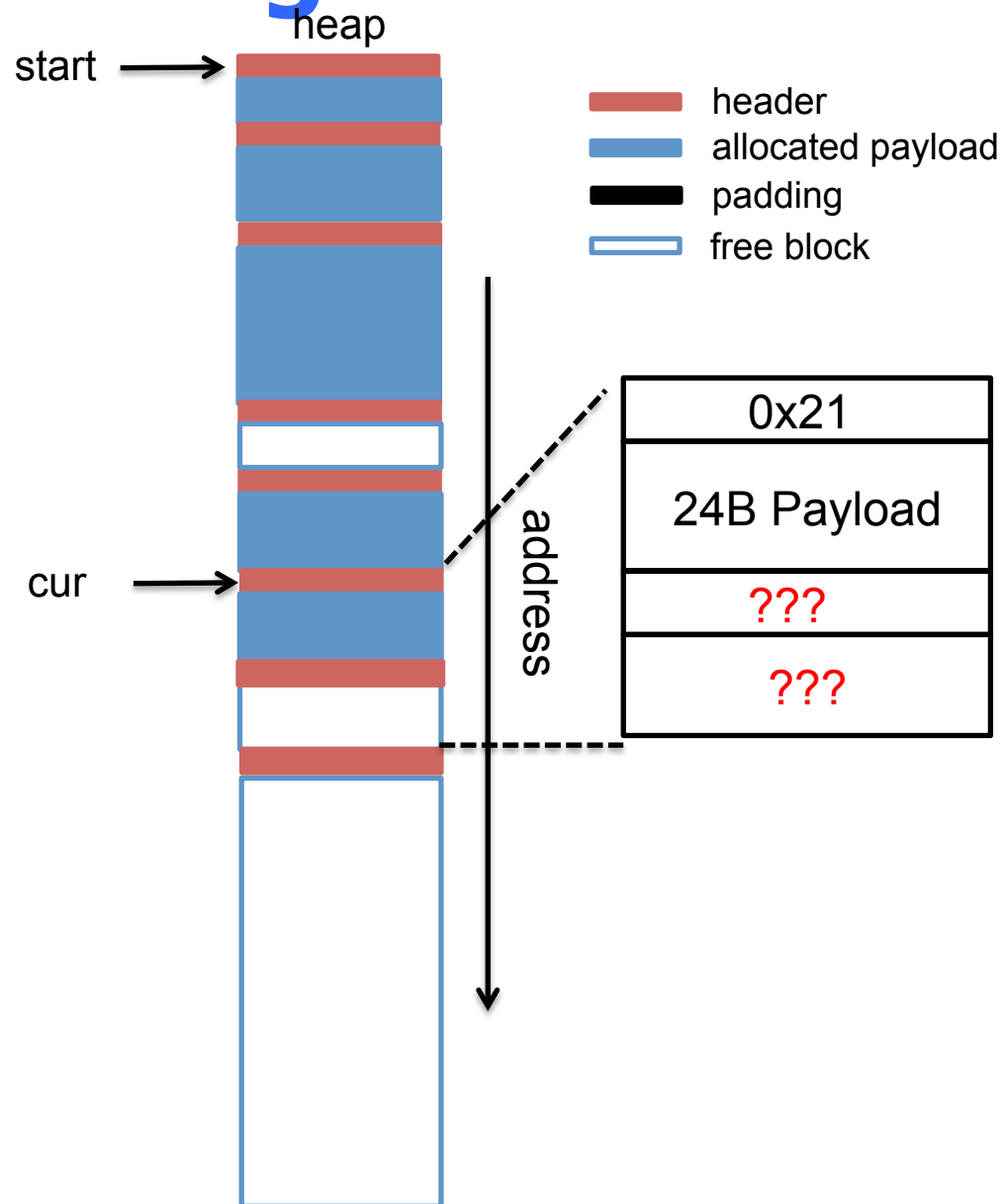
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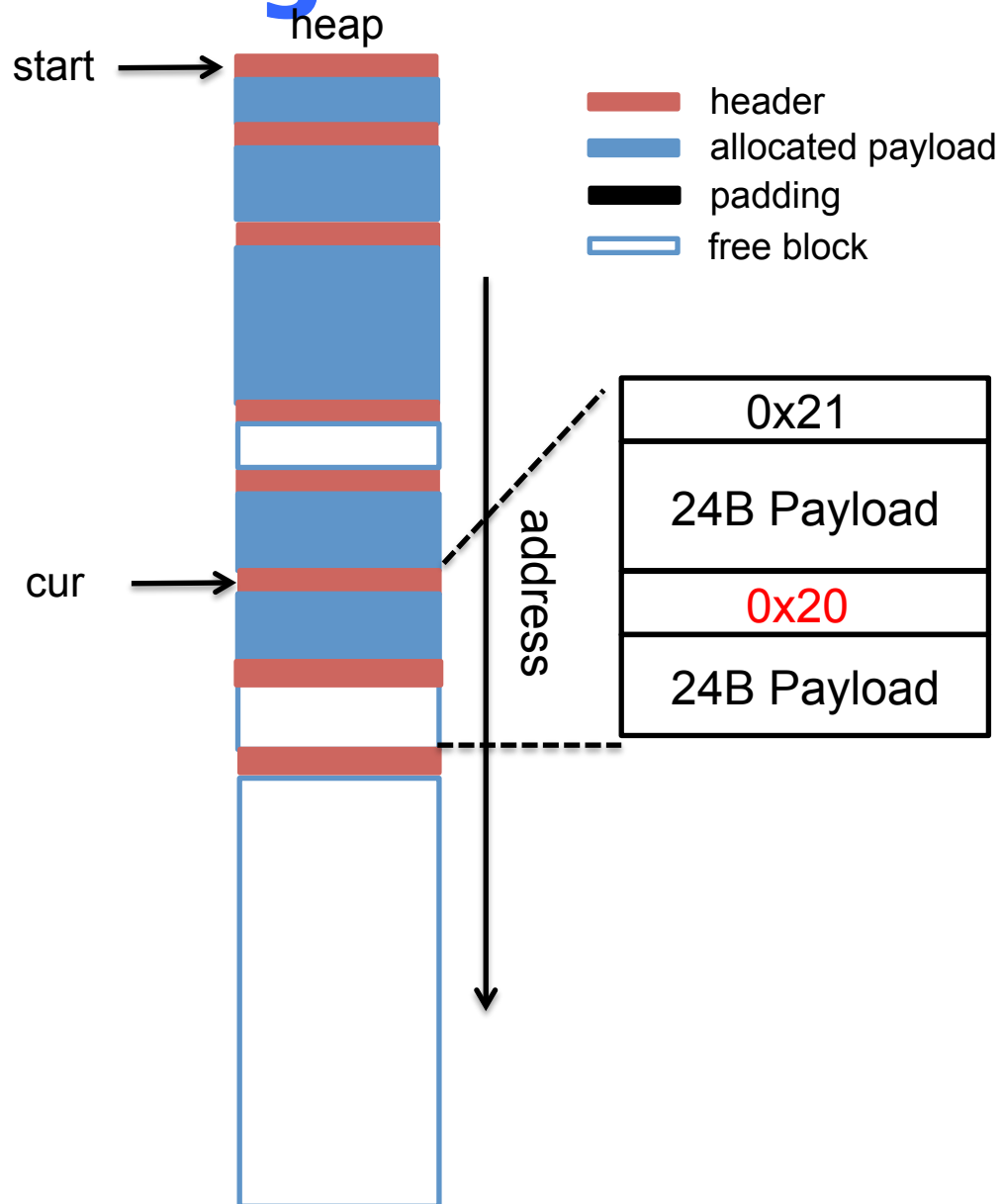
Splitting free block

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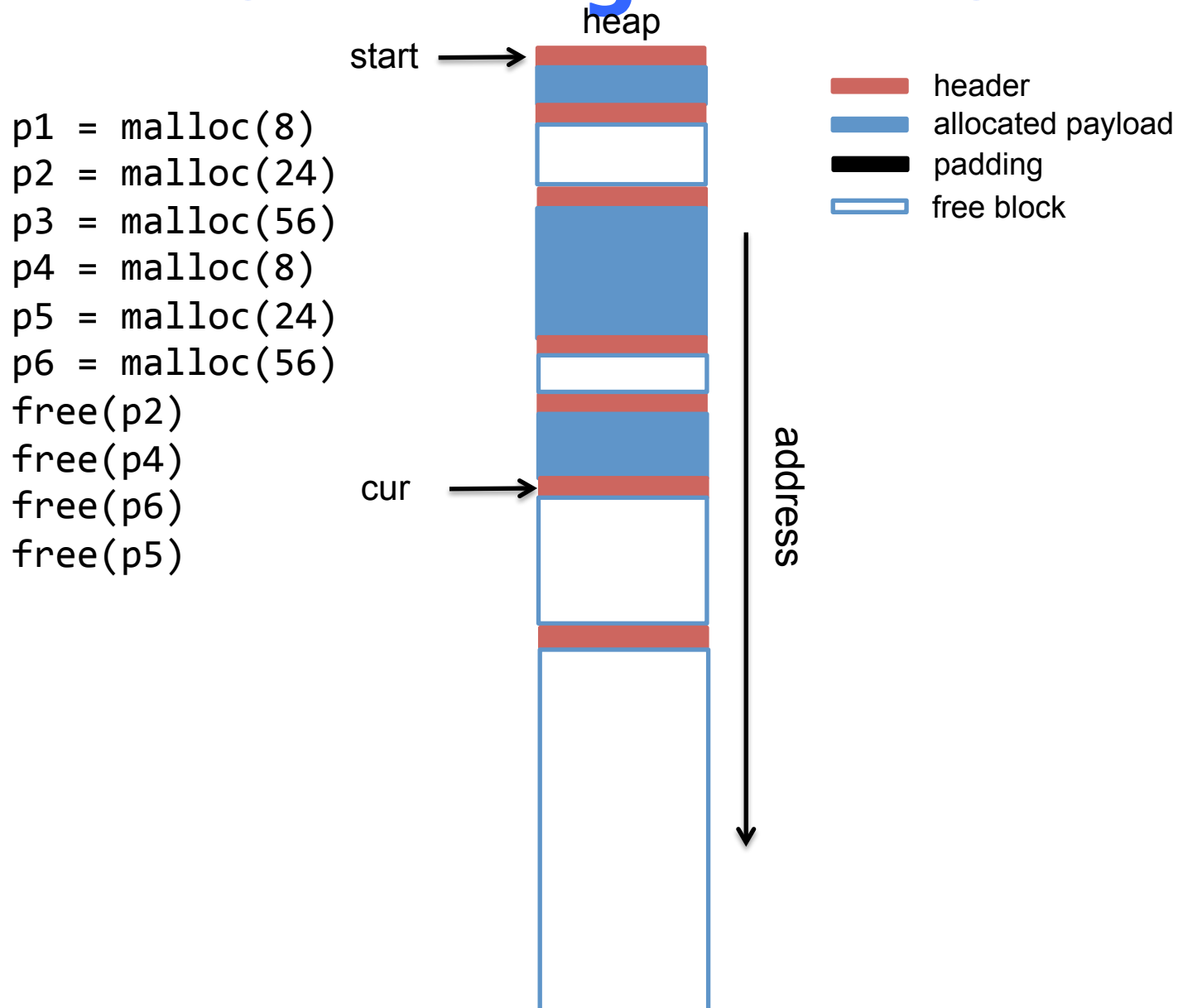


Splitting free block

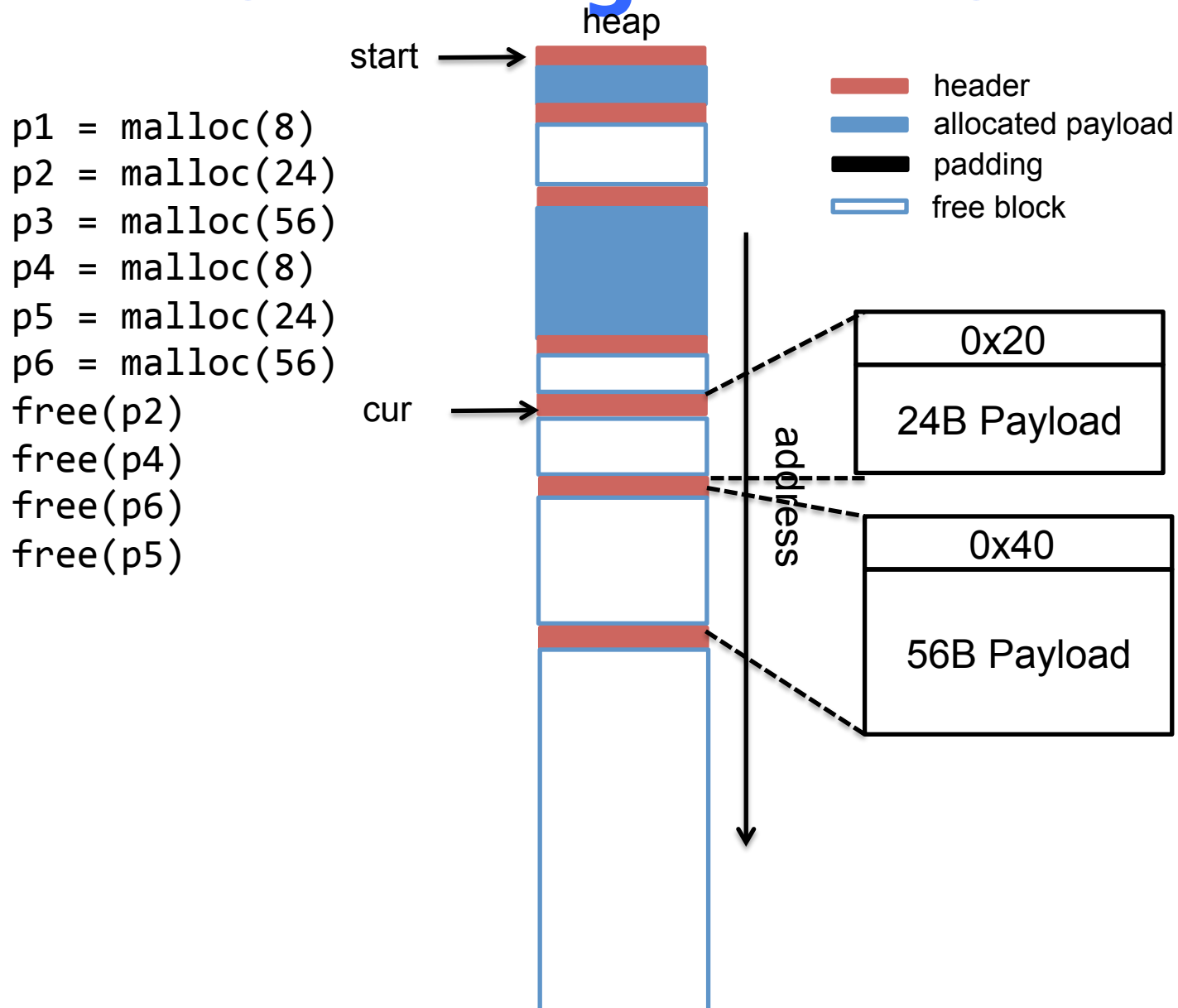
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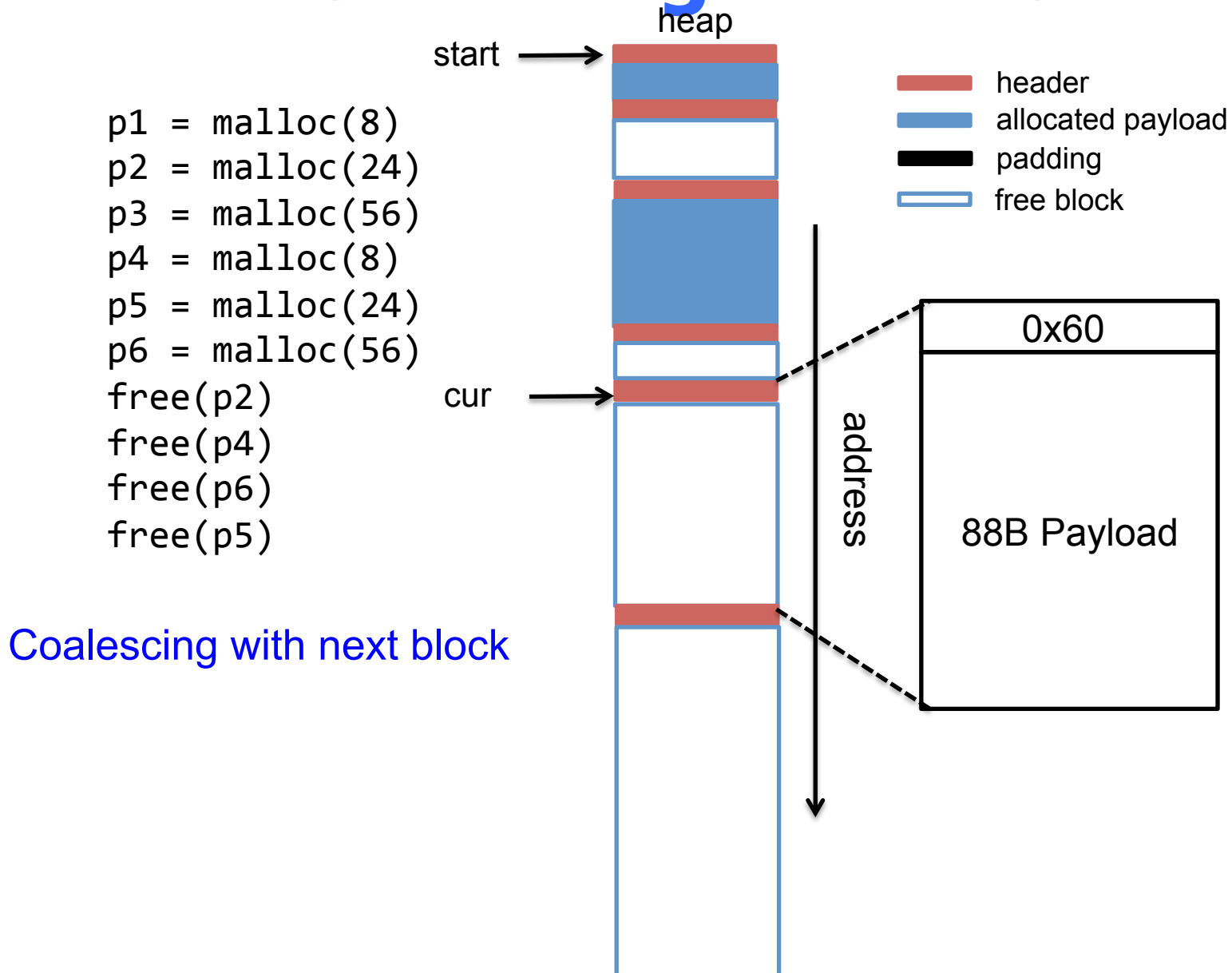
Coalescing free blocks



Coalescing free blocks

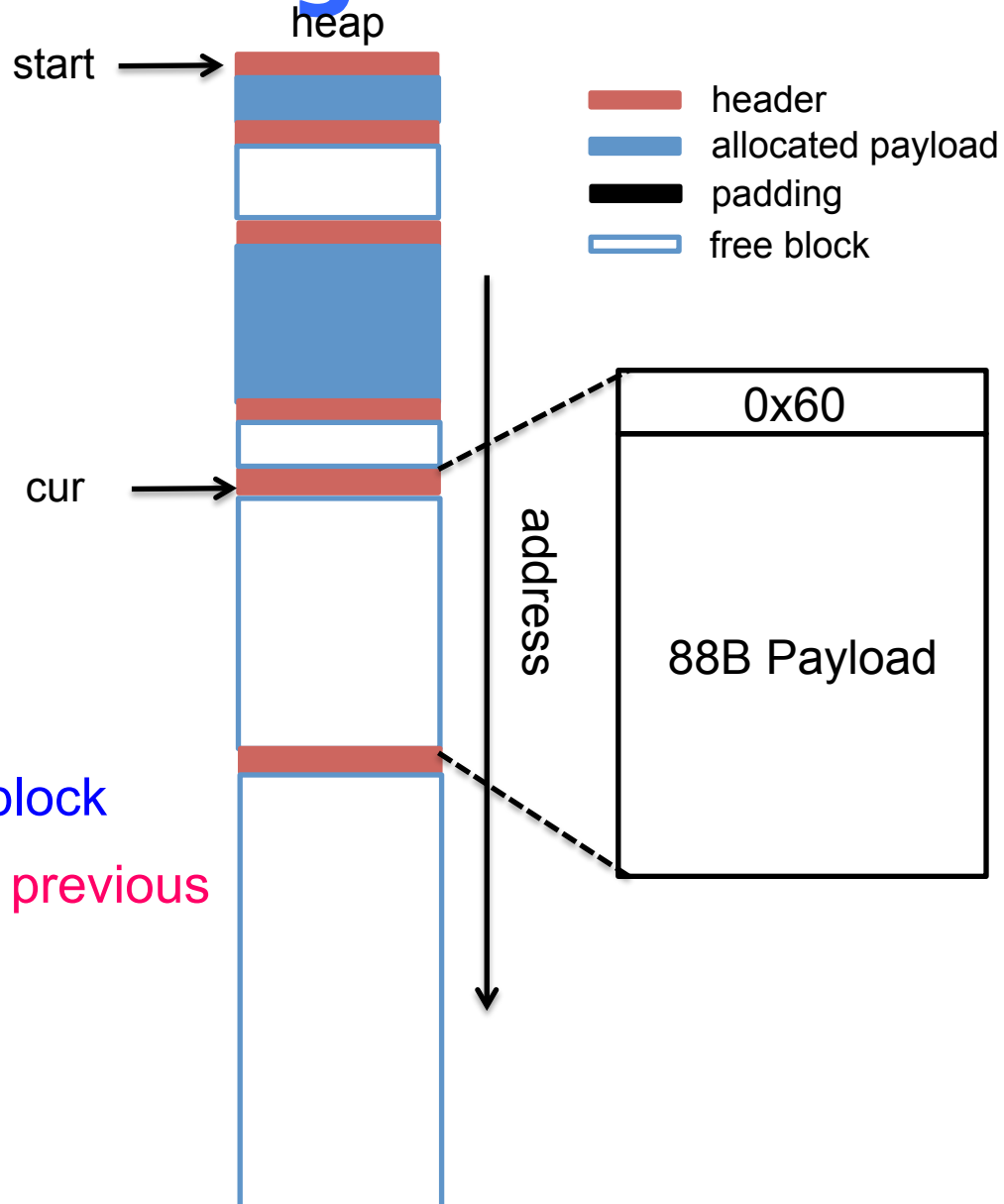


Coalescing free blocks



Coalescing free blocks

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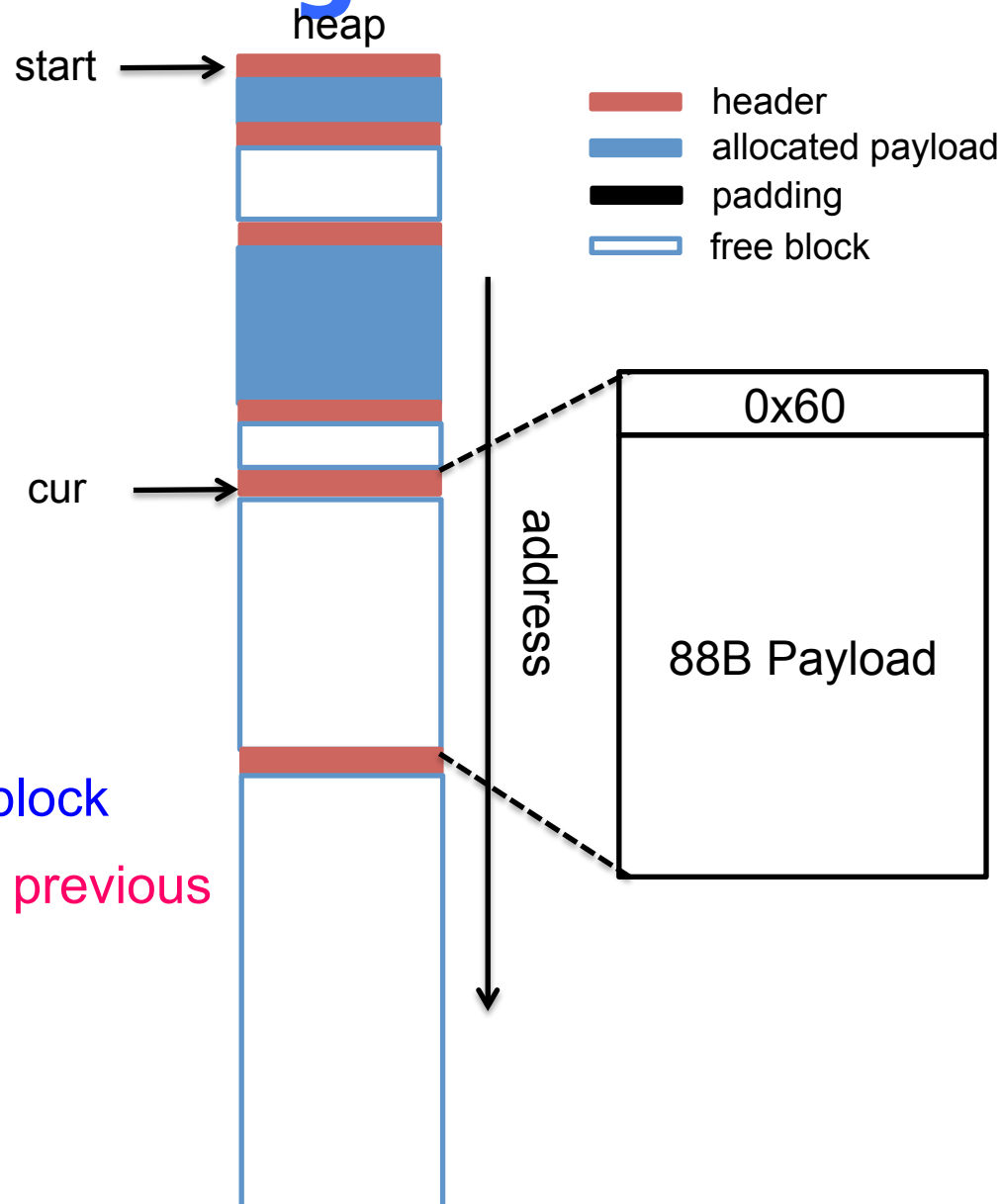


Coalescing with next block

How to coalesce with previous block?

Coalescing free blocks

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```



Coalescing with next block

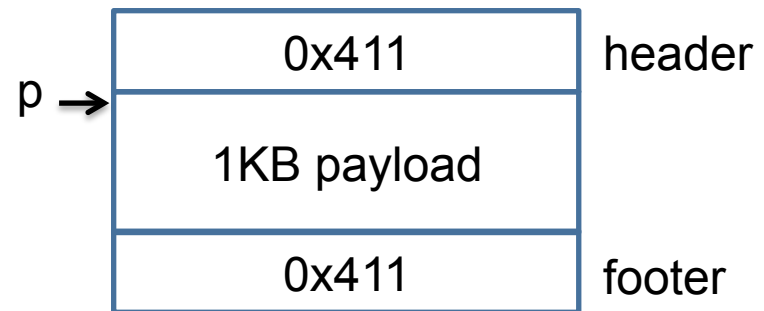
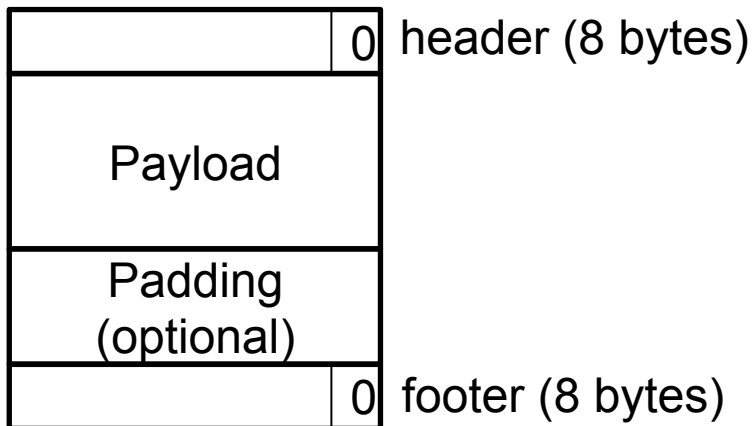
How to coalesce with previous block?

-- search from start?

Coalescing free blocks

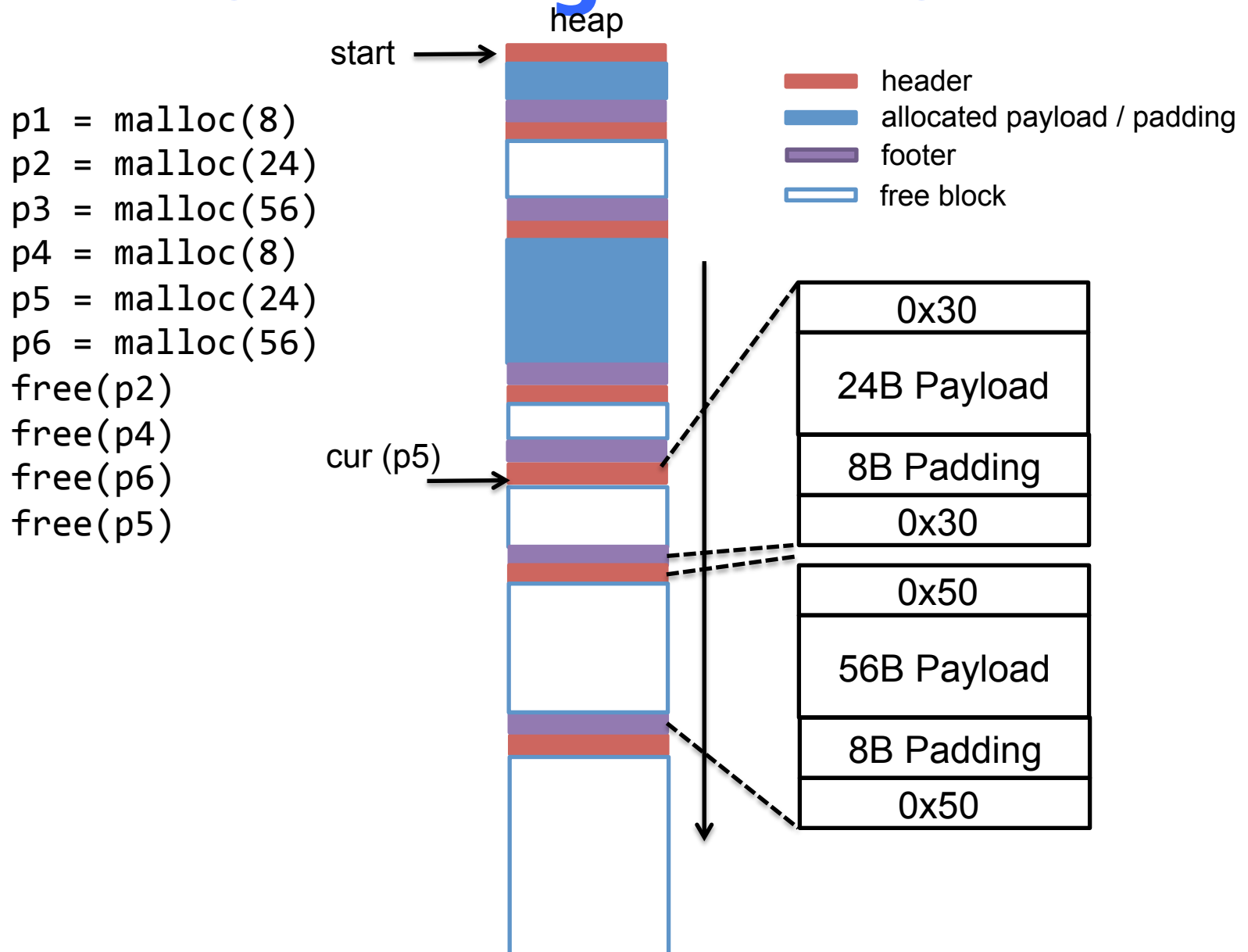
Embed the metadata in the chunks (blocks)

- Each block has a one-word (8 bytes) header and (8 bytes) footer
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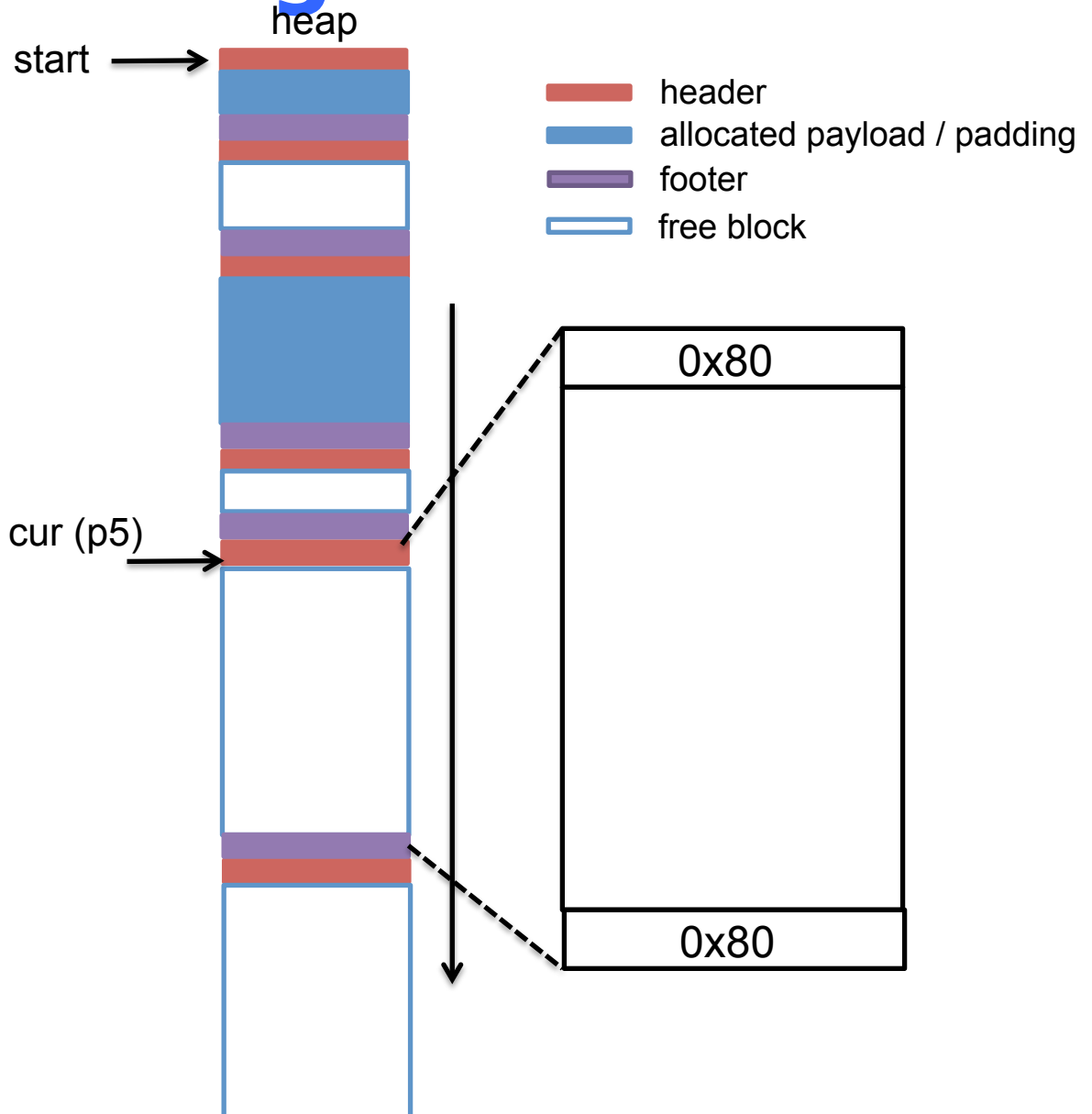
```
p = malloc(1024)
```

Coalescing free blocks

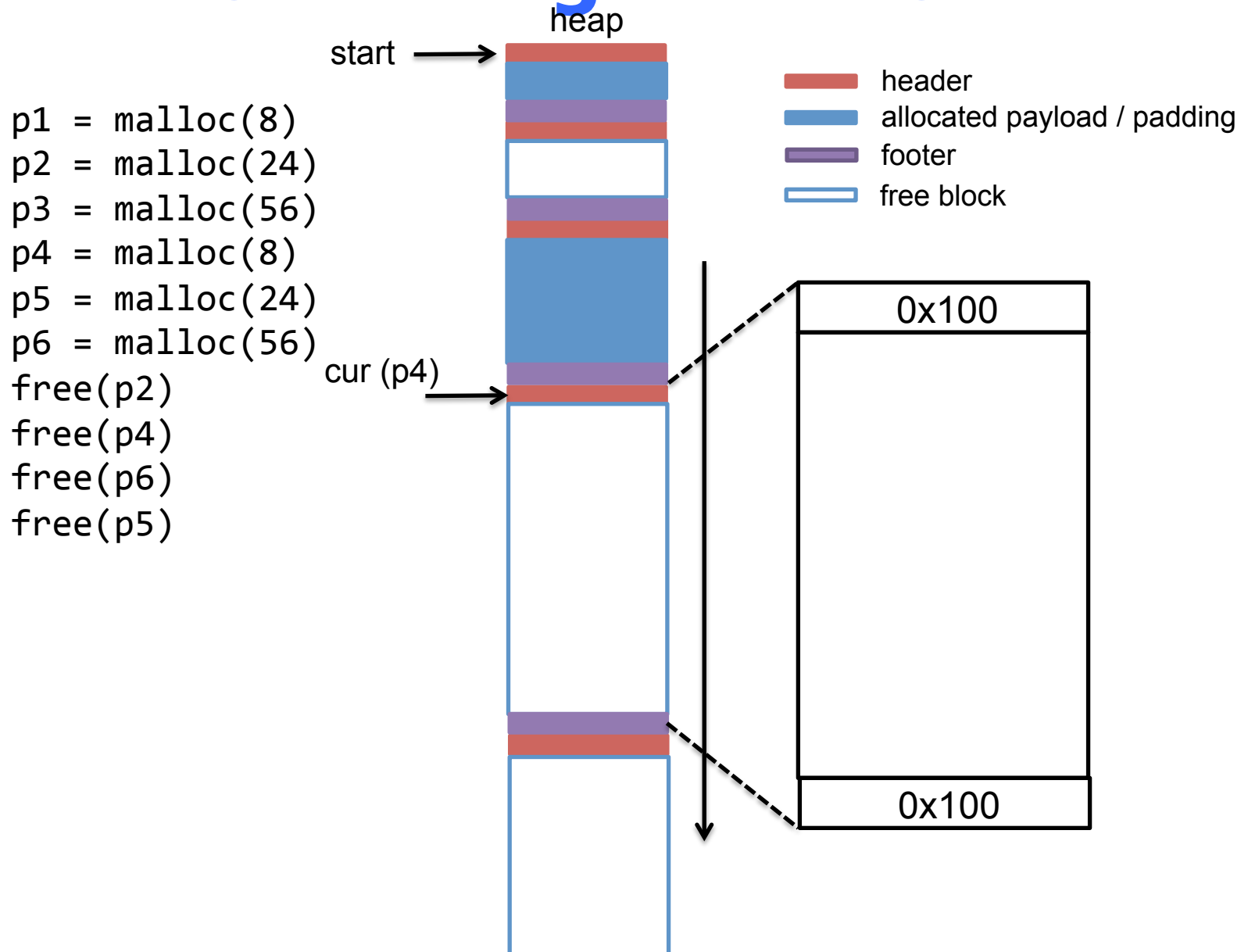


Coalescing free blocks

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Coalescing free blocks



Exercises

| Alignment | Request | Block size | Header (hex) |
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| 8 bytes | malloc(5) | | |
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Each block has both header and footer

Exercises

| Alignment | Request | Block size | Header (hex) |
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| 8 bytes | malloc(5) | 24 | 0x19 |
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Each block has both header and footer

Explicit free lists

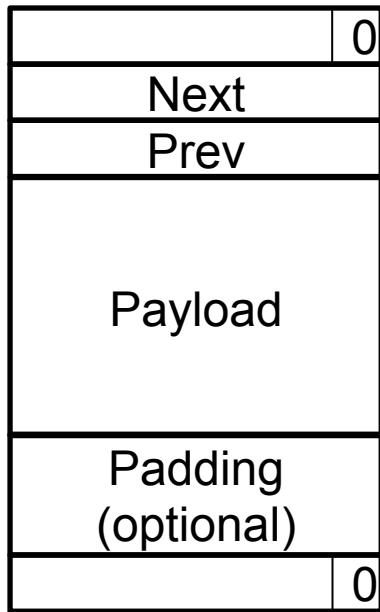
Problems of implicit free list

- Block allocation time is linear in the total number of heap blocks

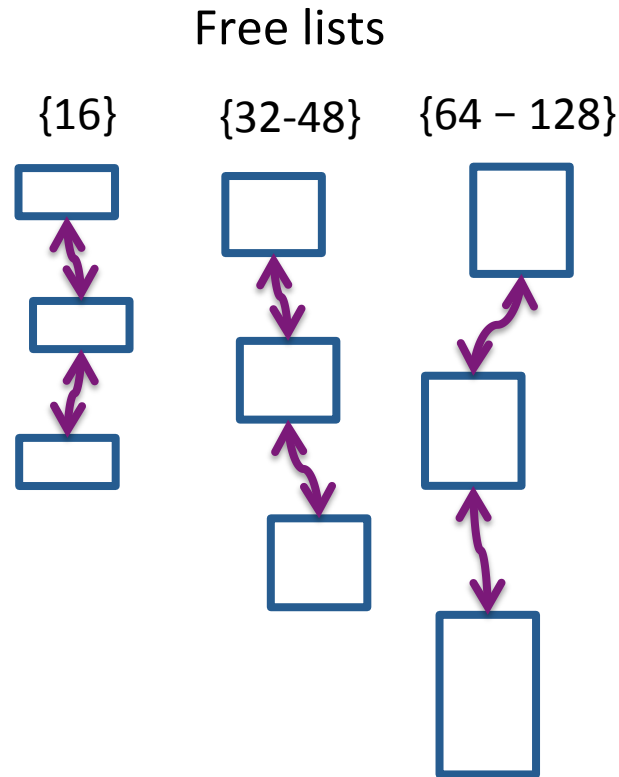
Basic idea – segregated list

- Maintain multiple free list, each list holds blocks that are roughly the same size

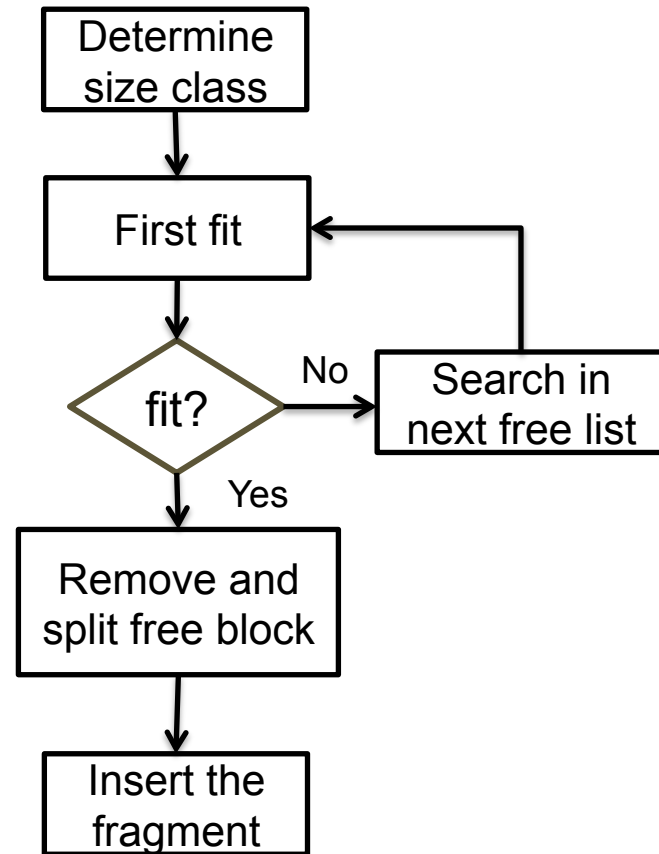
Segregated list



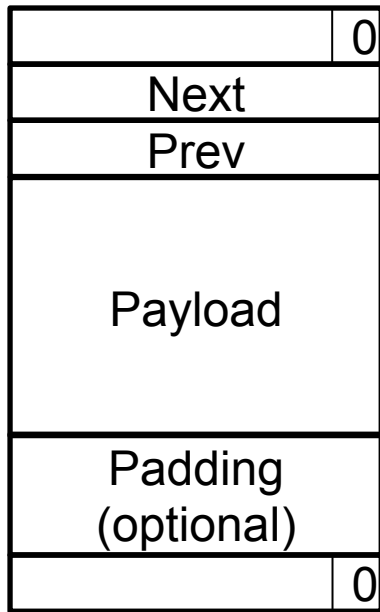
Block layout



Free lists

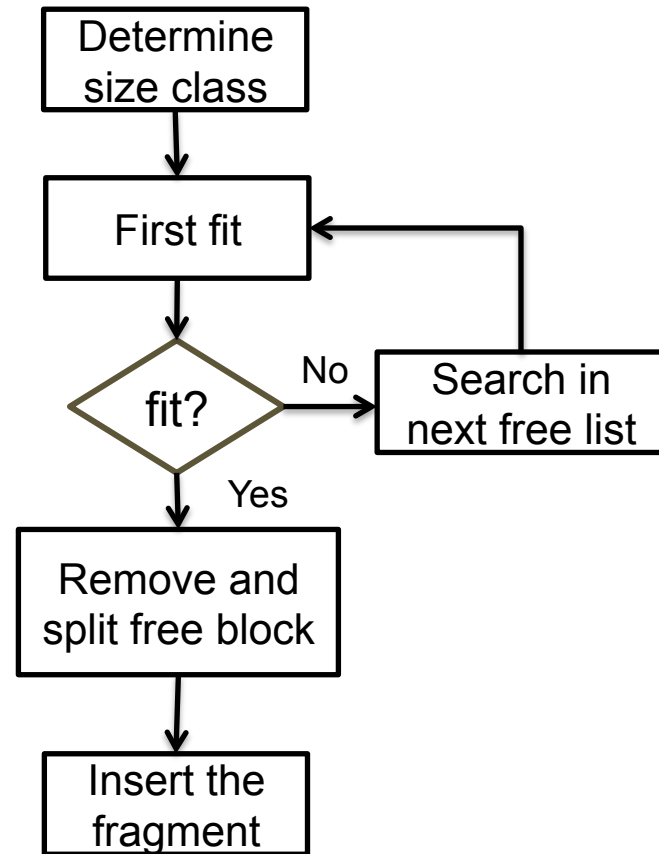
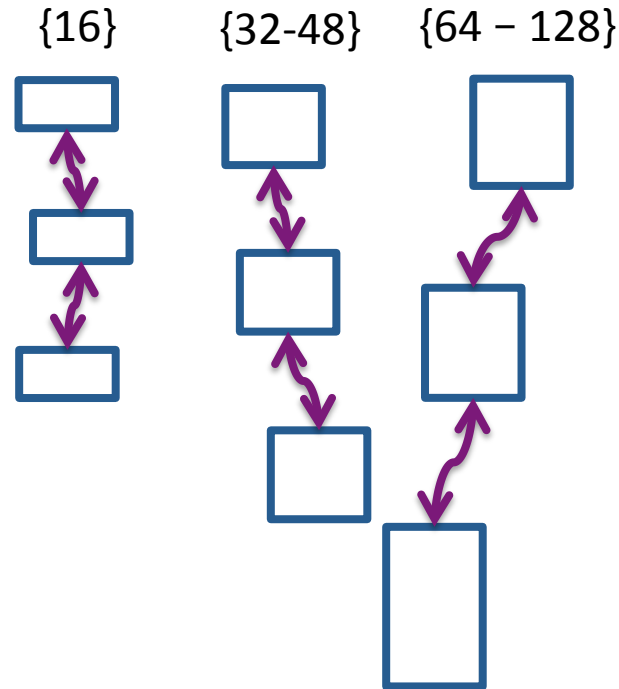


Segregated list



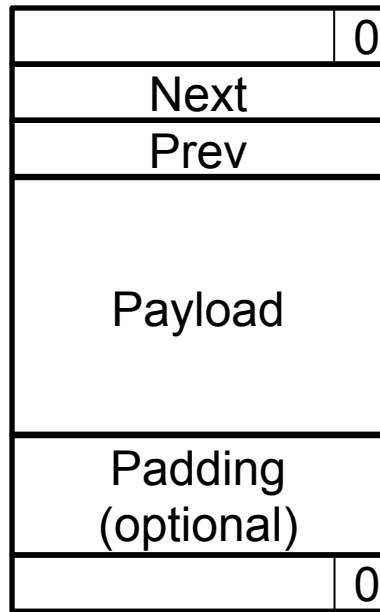
Block layout

Free lists



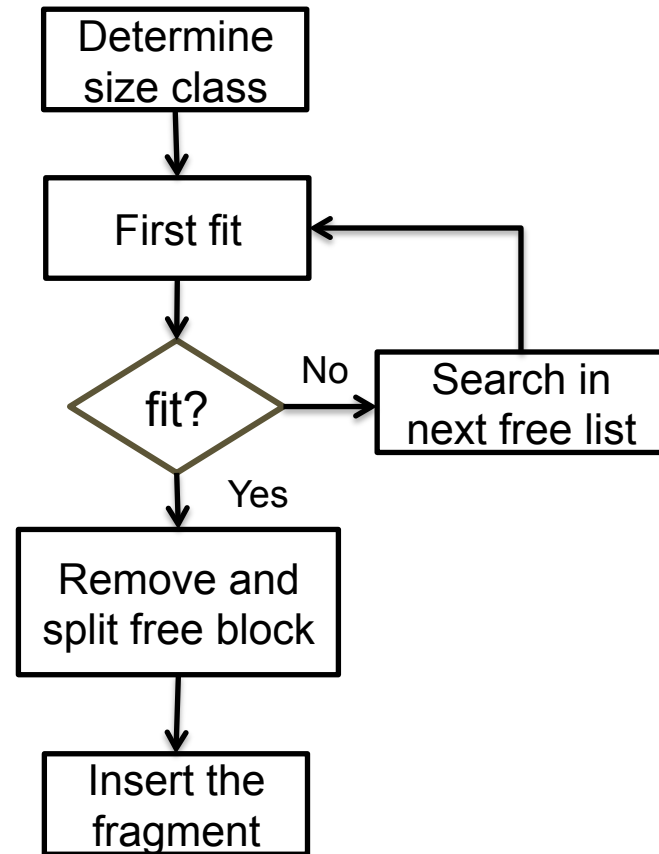
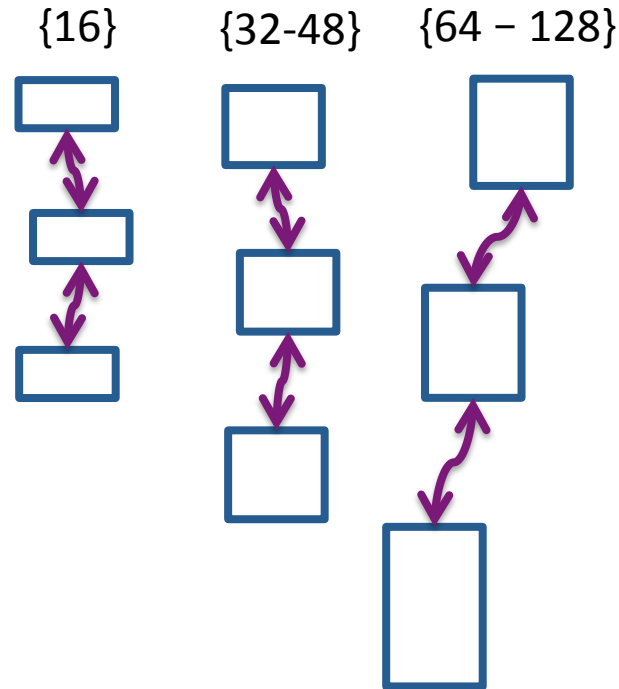
Do we need an allocated lists?

Segregated list



Block layout

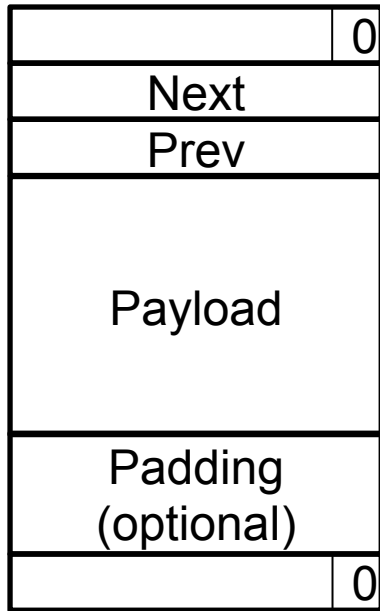
Free lists



Do we need an allocated lists?

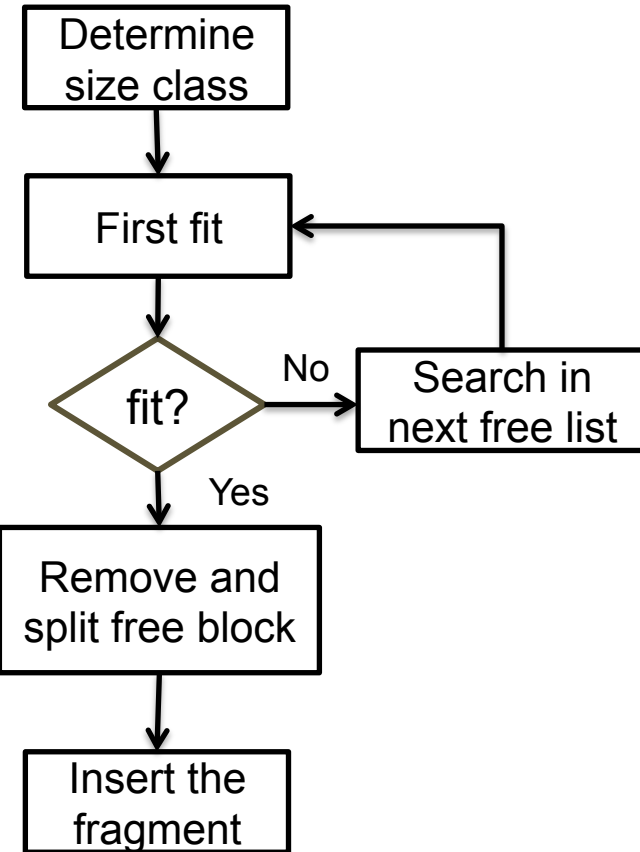
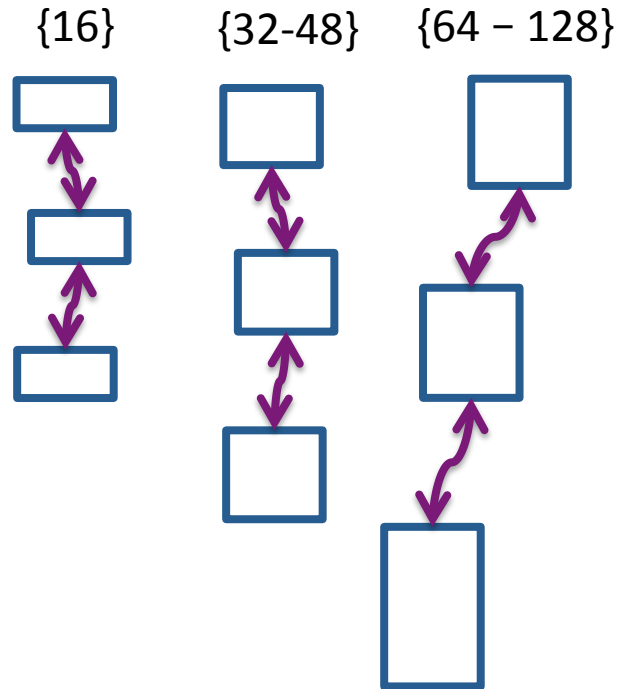
No, we are able to calculate the start of the block with p passed by free()

Segregated list



Block layout

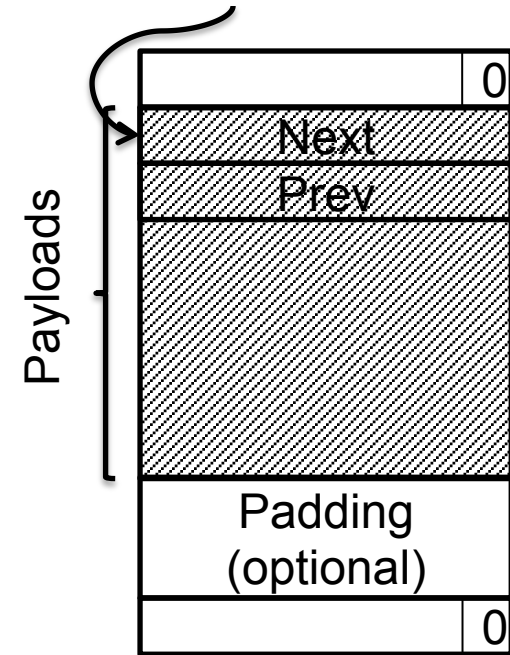
Free lists



Can we get rid of Next and Prev?

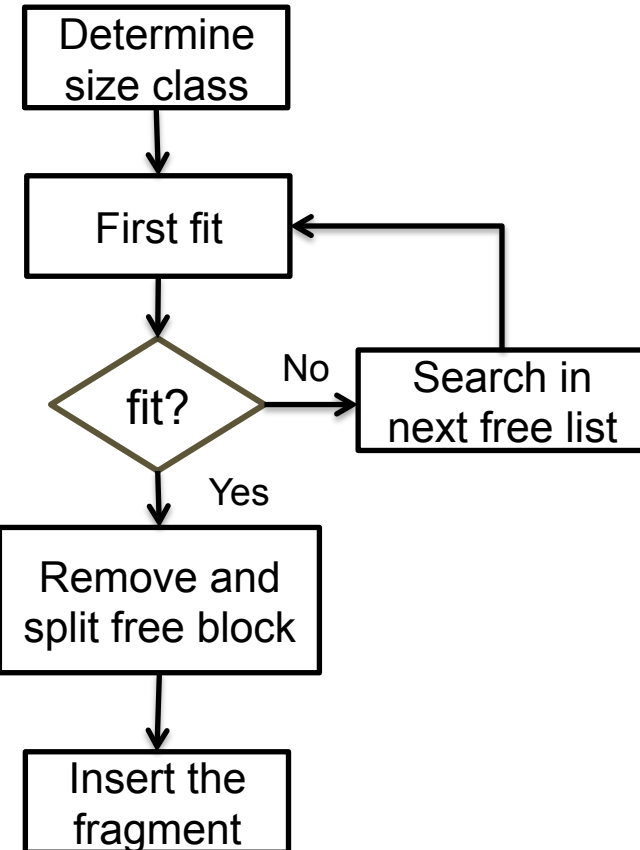
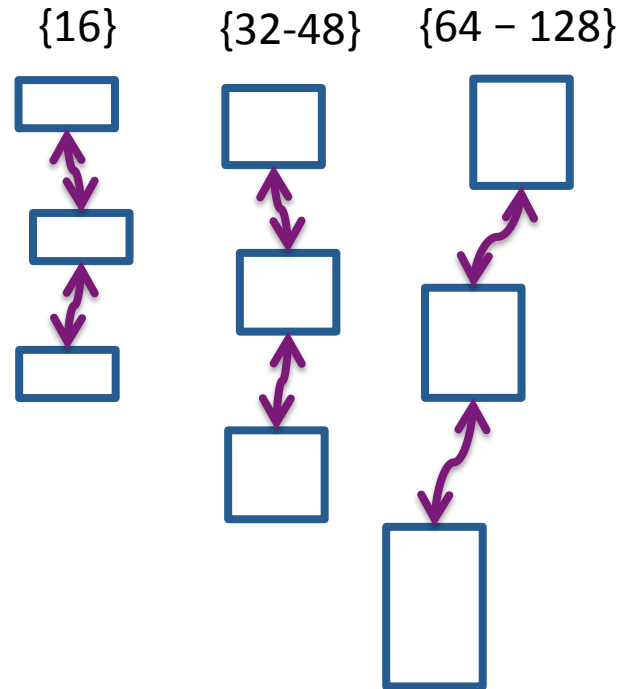
Segregated list

Addr returned to user



Block layout

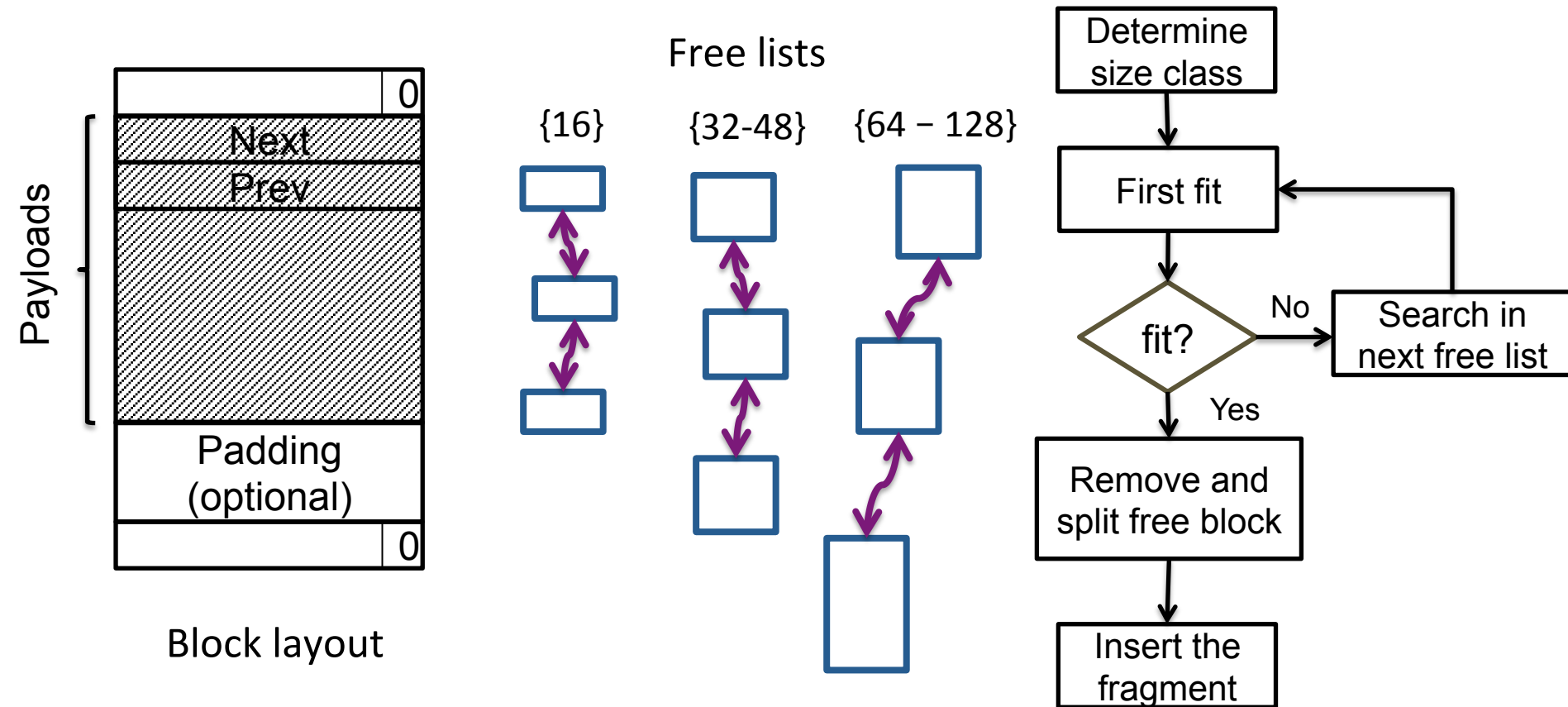
Free lists



Can we get rid of Next and Prev?

Allocated blocks do not need Next and Prev

Segregated list



With this design, what is the minimal size for a free block?

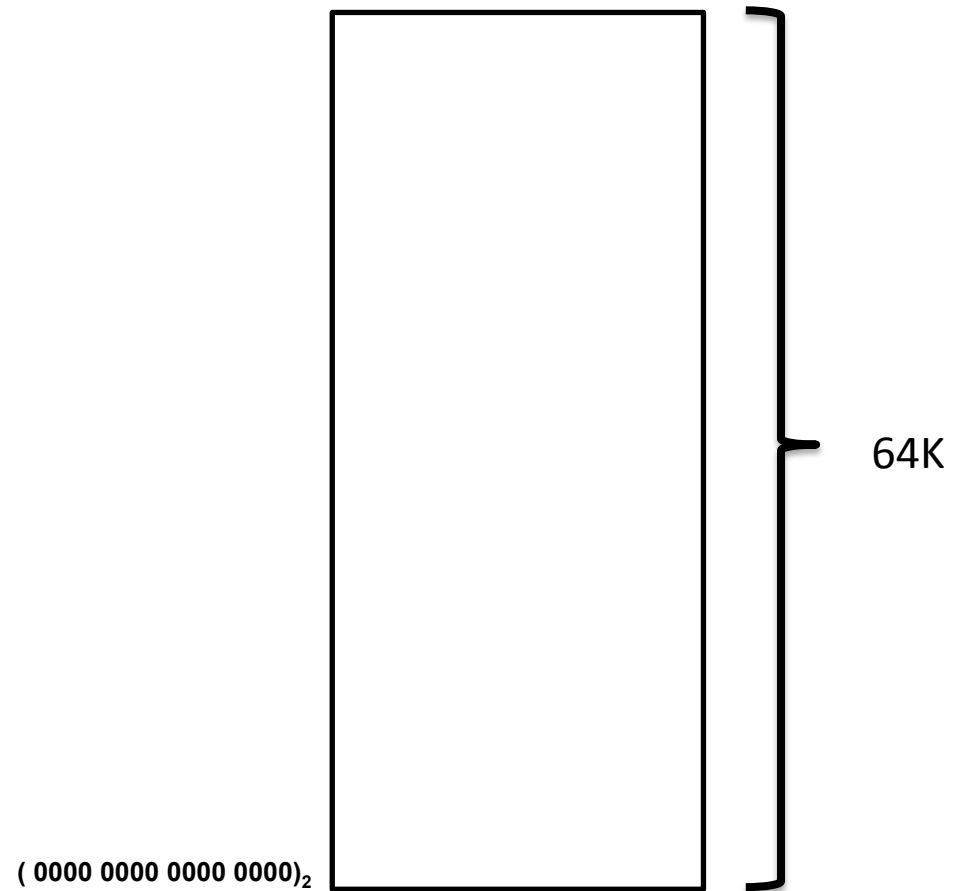
Buddy System

Adopted by Linux kernel and jemalloc

This lecture

- A simplified binary buddy allocator

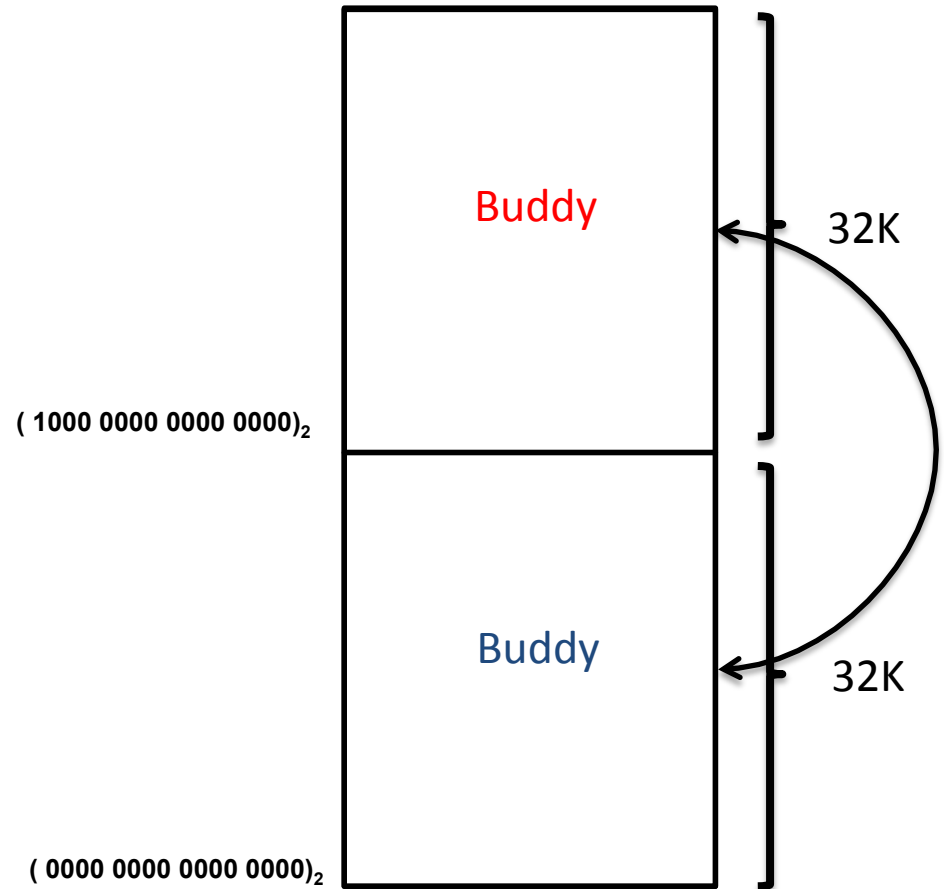
Binary buddy system



Binary buddy system

Split

- Split exactly in half



Binary buddy system

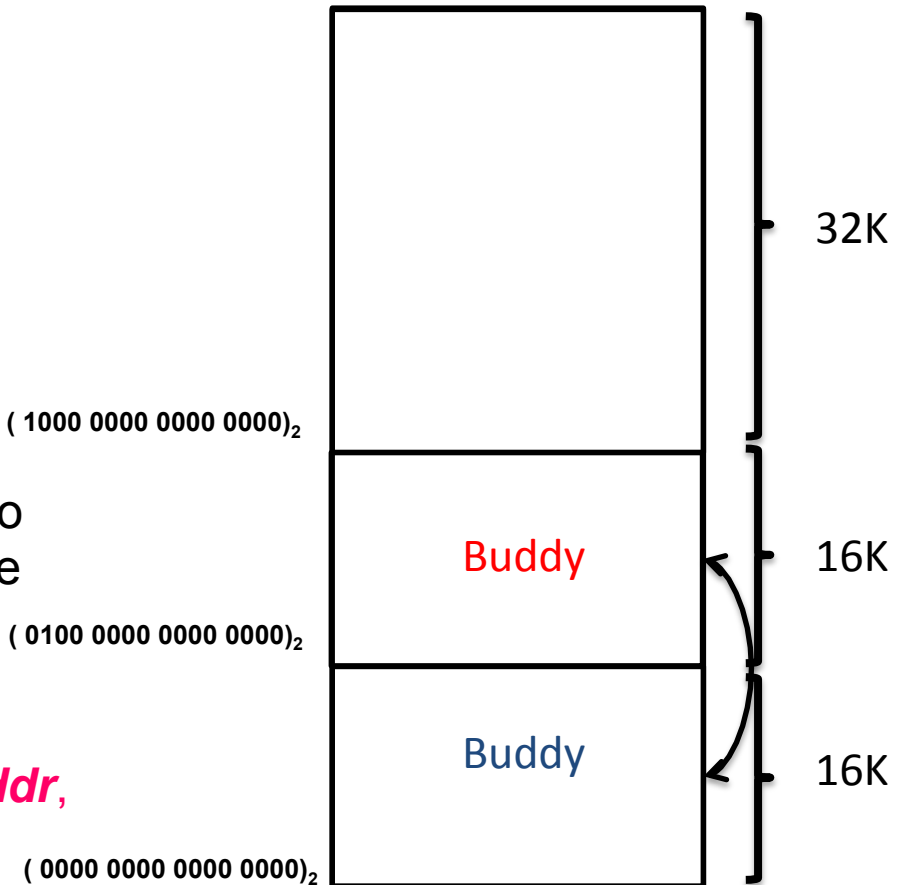
Split

- Split exactly in half
- Each half is the buddy of the other

Address

- Block of size 2^n begin at memory addresses where the n least significant bits are zero
- When a block of size 2^{n+1} is split into two blocks of size 2^n , the addresses of these two blocks will differ in exactly one bit, bit n .

If a block of size 2^n begins at address **addr**, what is its buddy address and size?



Binary buddy system

Split

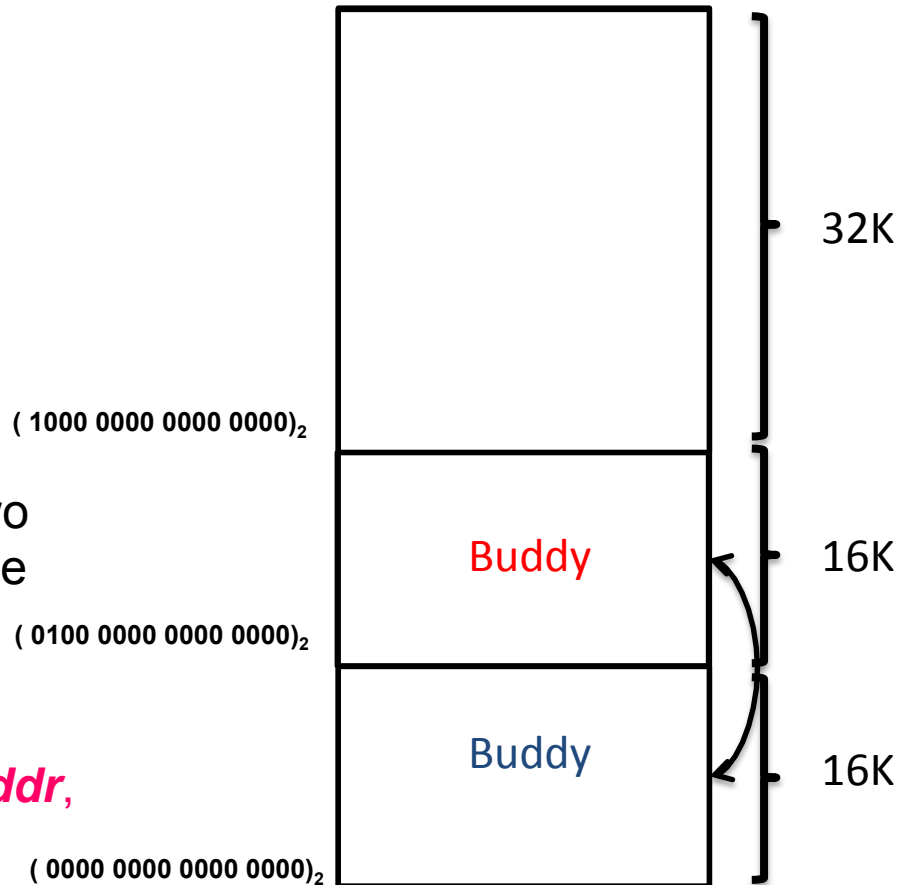
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If a block of size 2^n begins at address **addr**,
what is its buddy address and size?

addr of buddy = $\text{addr} \oplus (1 \ll n)$



Binary buddy system

Split

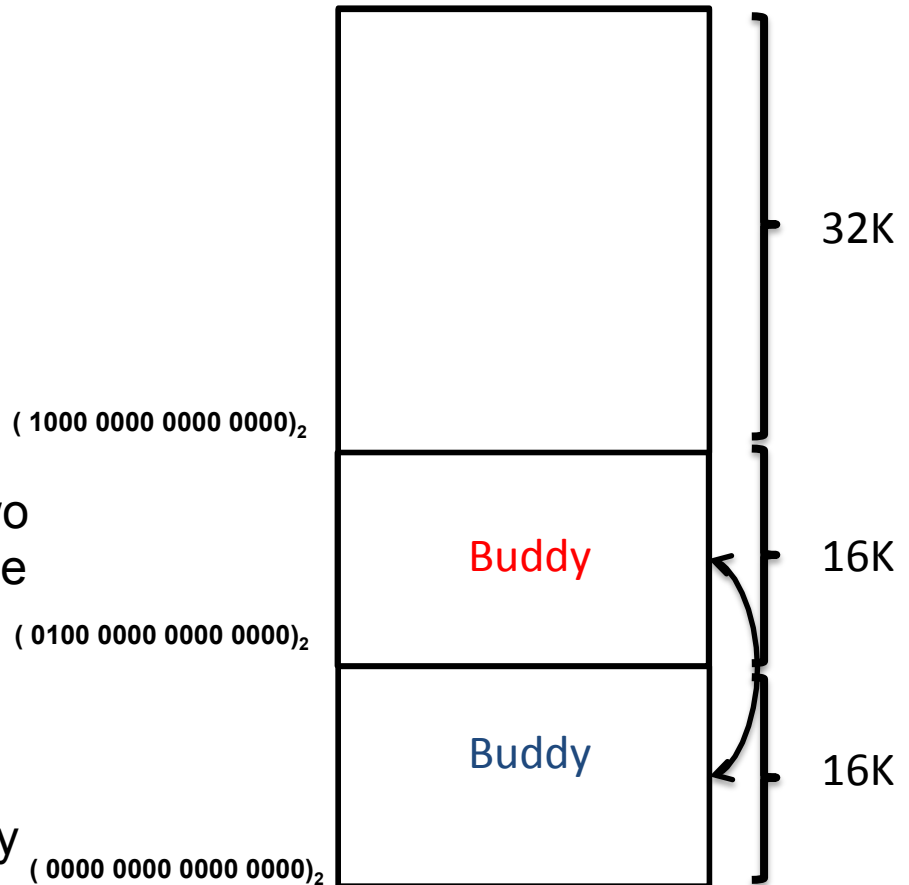
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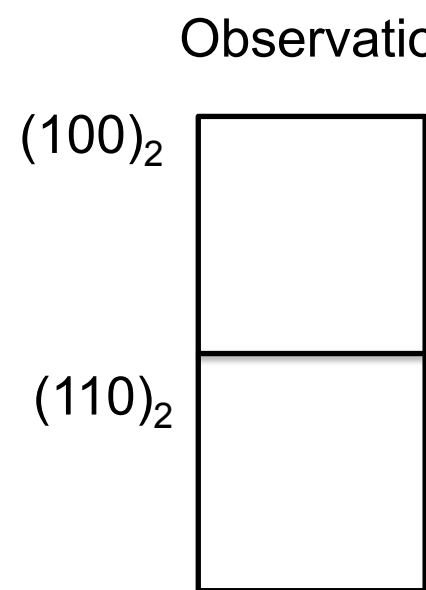
Combine

- We assume only combine with its buddy block in our lecture

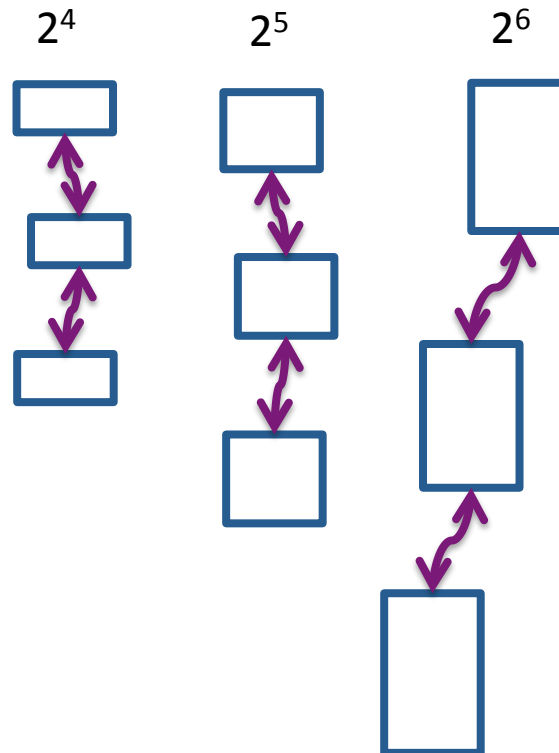


Buddy system

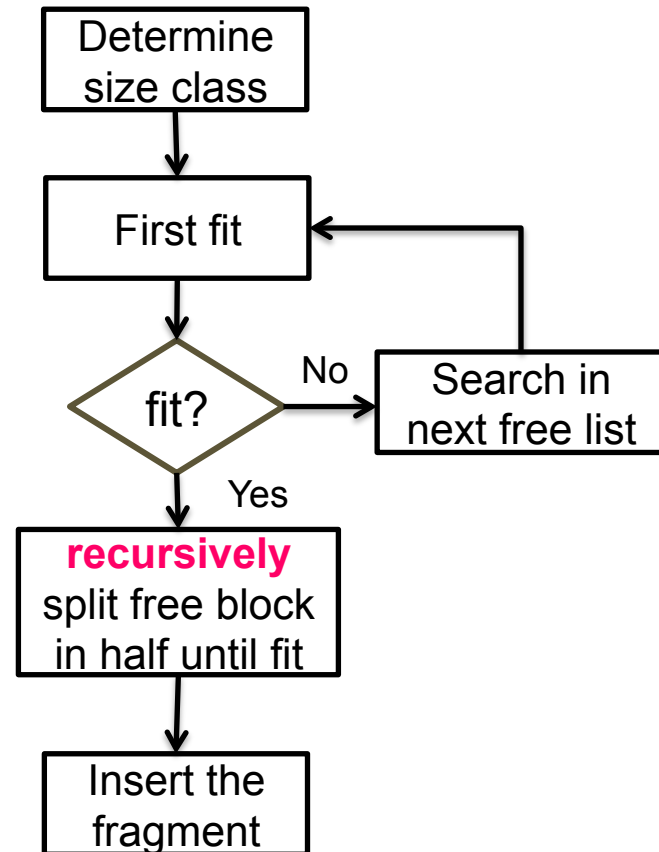
Observation



Free lists



Each list has the same size of blocks which is a power of 2.

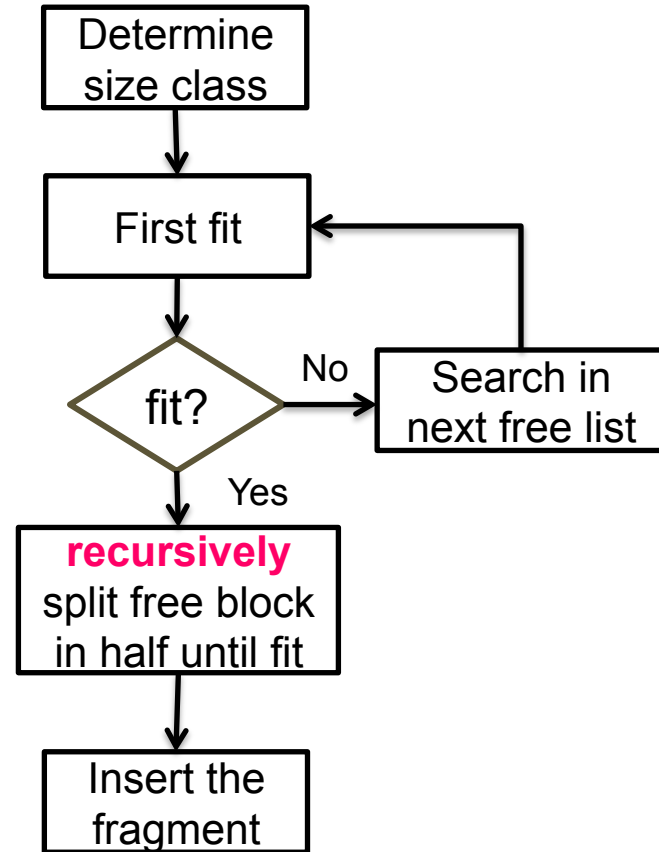
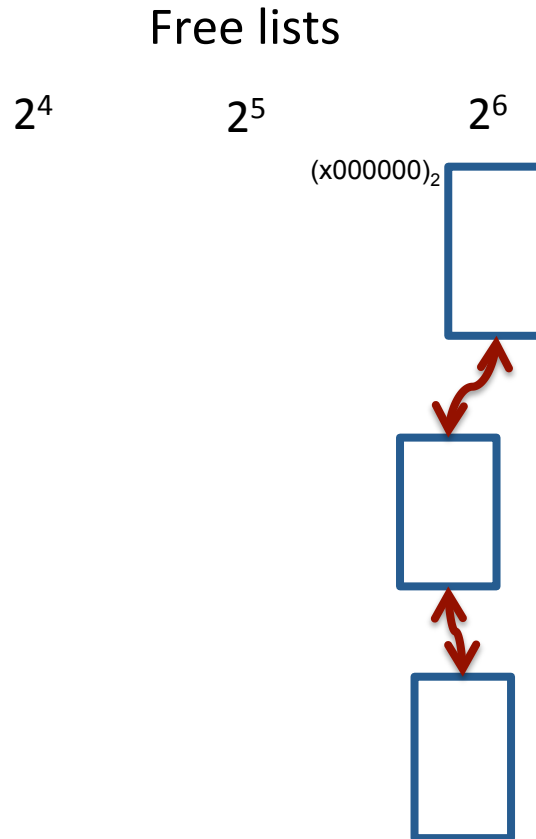


Buddy system

`p = malloc(1)`

Step 1. search in 2^6 list

Step 2. recursive split



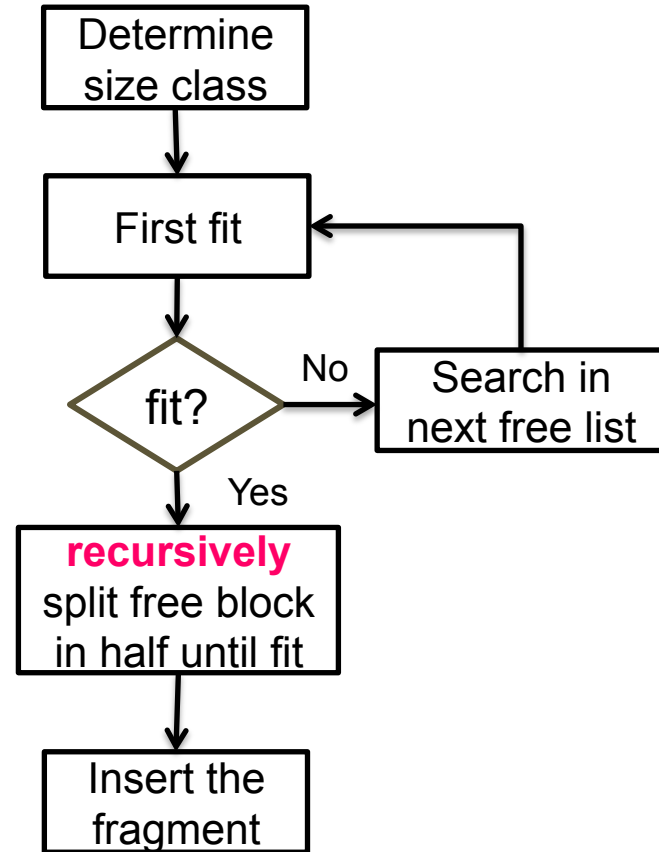
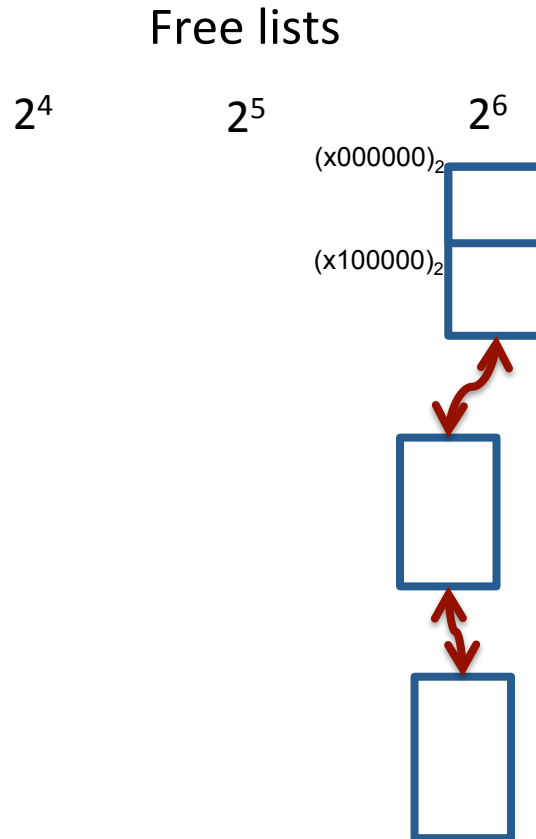
Each list has the same size of blocks which is a power of 2.

Buddy system

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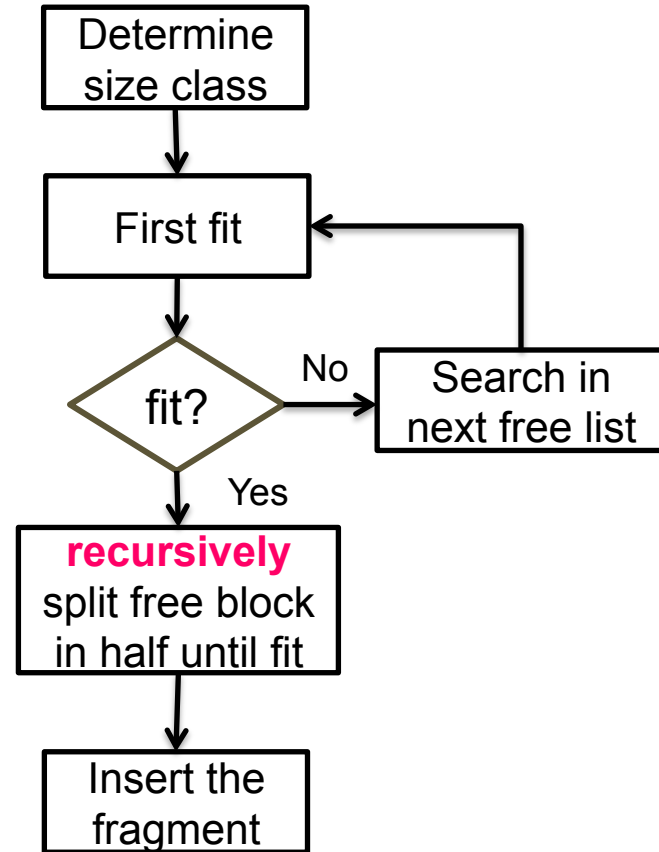
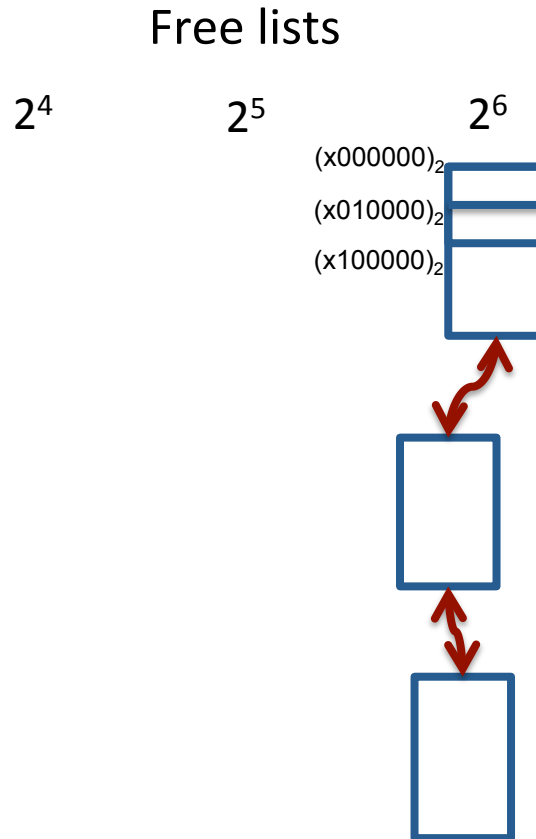


Buddy system

`p = malloc(1)`

Step 1. search in 2^6 list

Step 2. recursive split

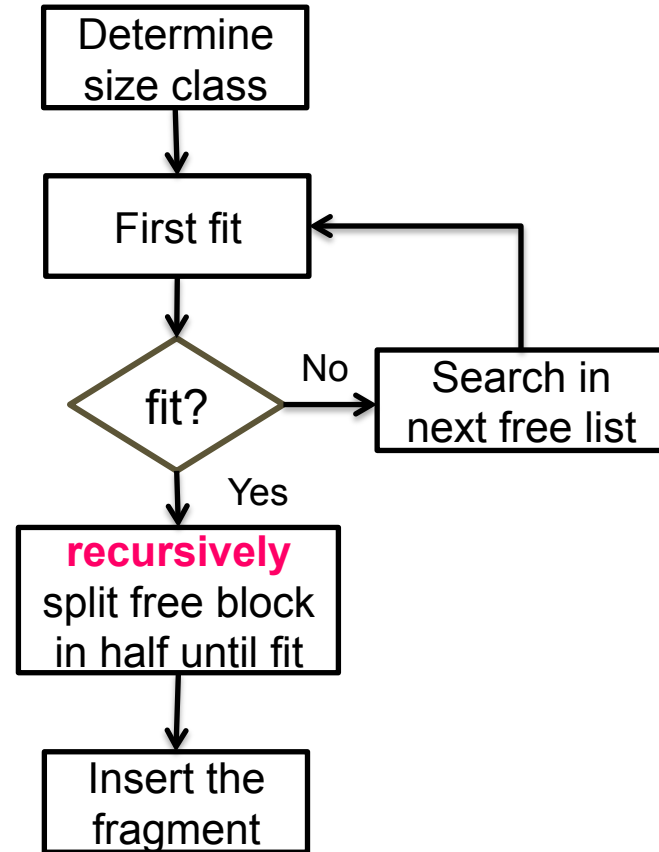
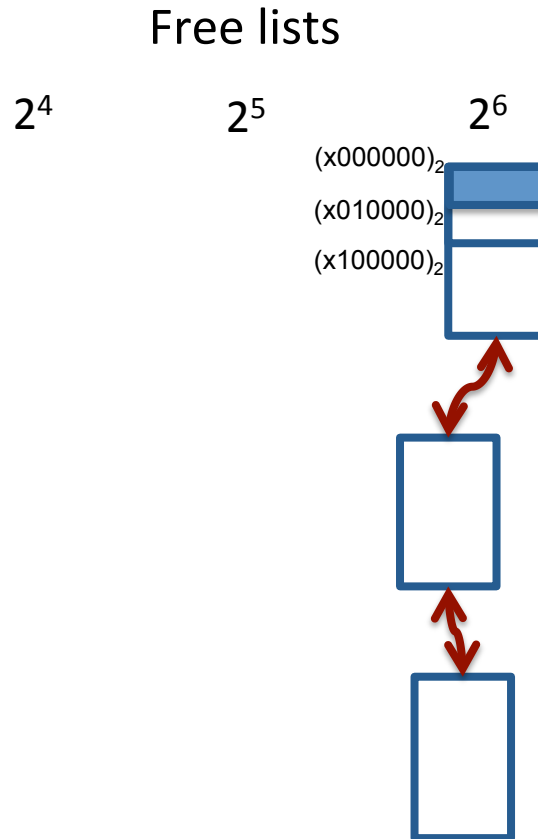


Buddy system

`p = malloc(1)`

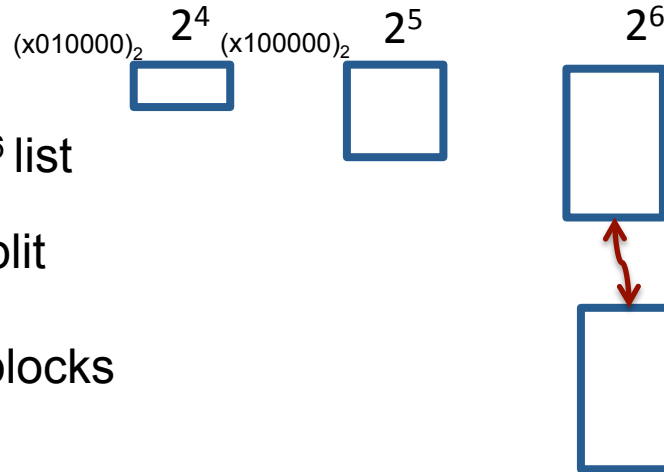
Step 1. search in 2^6 list

Step 2. recursive split



Buddy system

`p = malloc(1)`

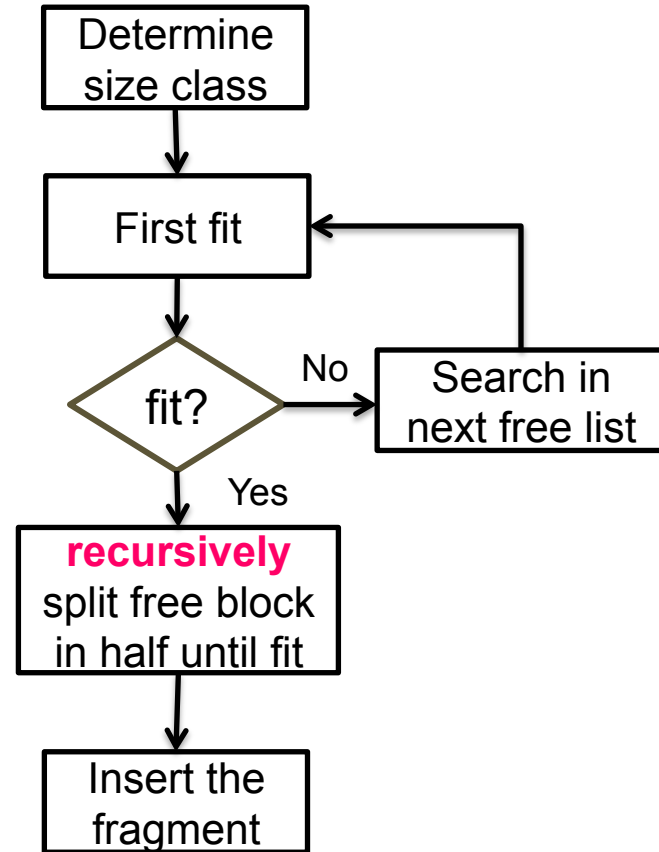


Step 1. search in 2^6 list

Step 2. recursive split

Step 3. insert free blocks
into the list

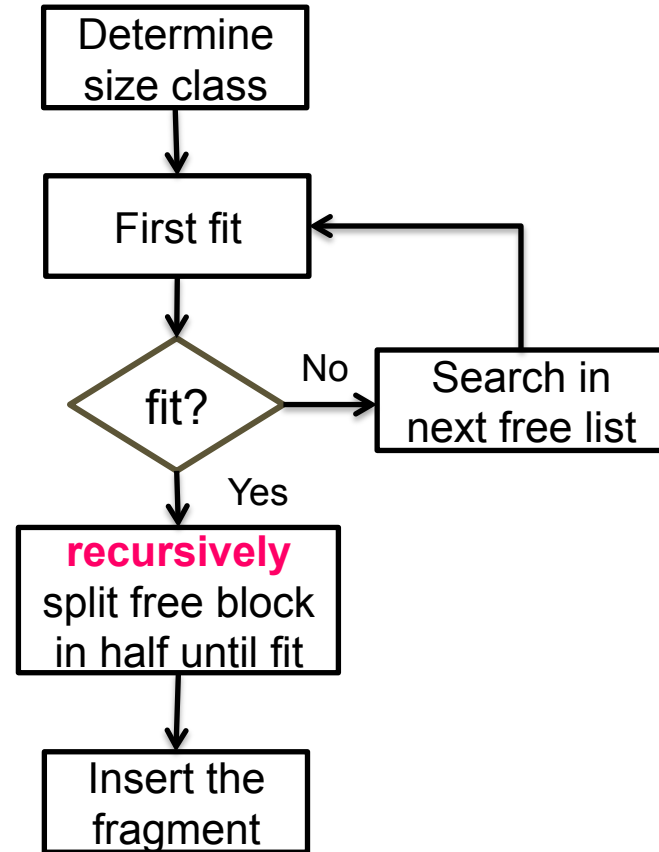
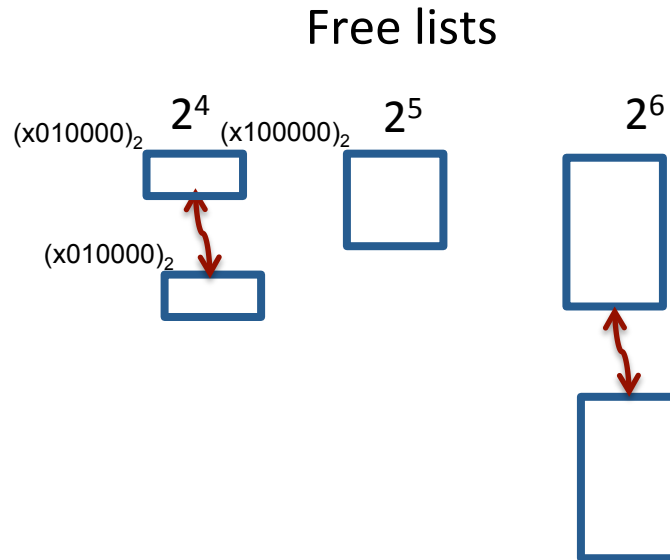
Step 4. return, p is $(x000000)_2$



Buddy system

`p = malloc(1)`

`free(p)`



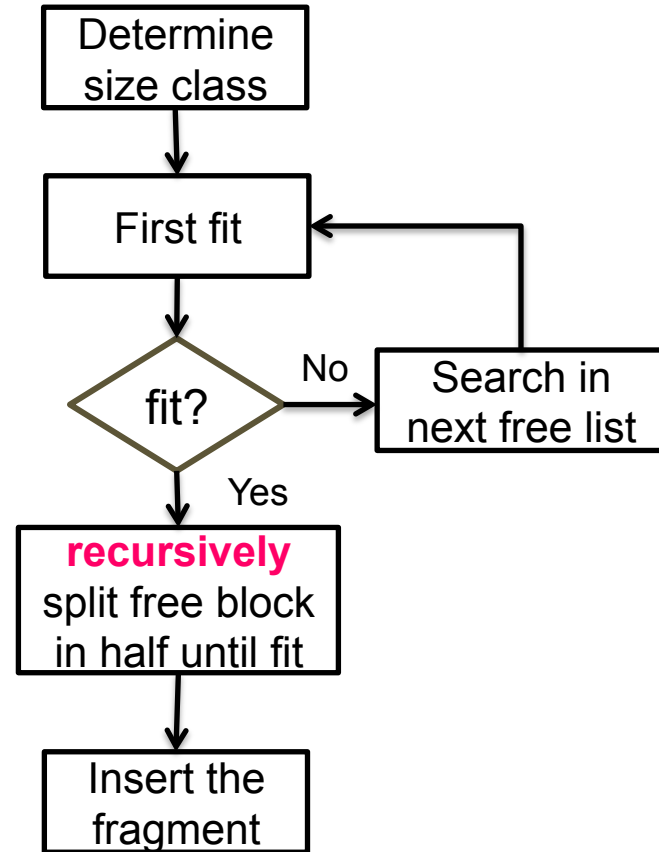
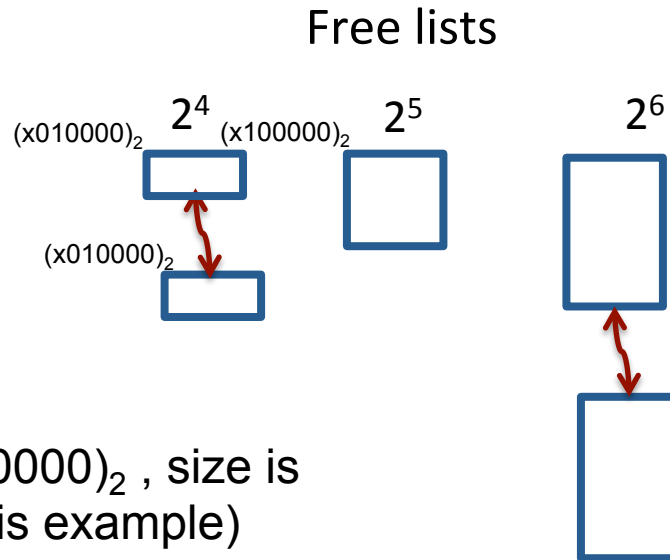
Buddy system

`p = malloc(1)`

`free(p)`

p's address is $(x000000)_2$, size is 16B (no footer in this example)

→ p's buddy is 16 B block begins at $x000000 \wedge (1 < 4)$ which is $(x010000)_2$



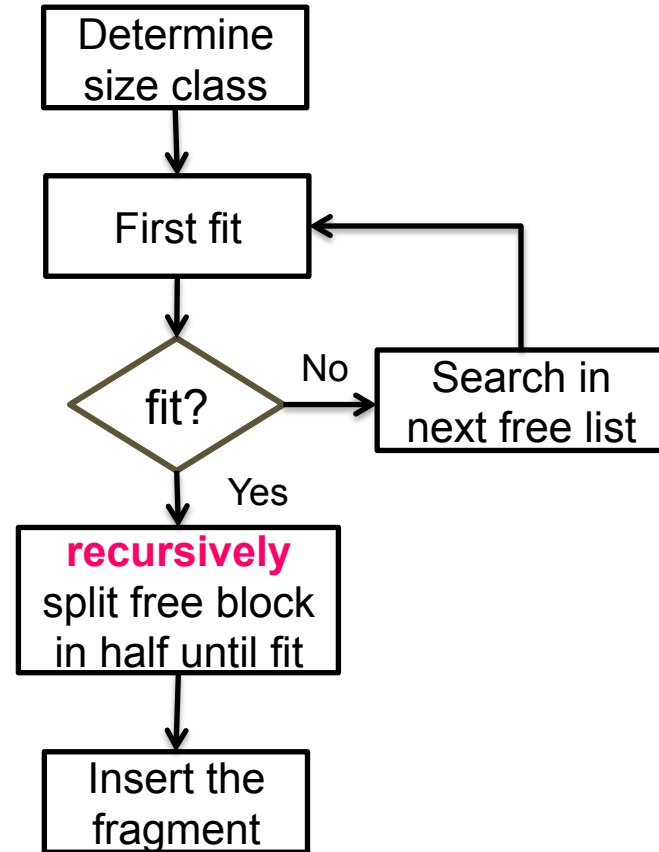
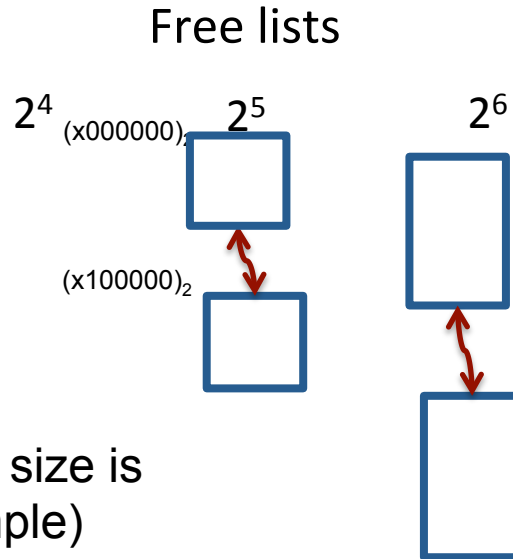
Buddy system

`p = malloc(1)`

`free(p)`

p's address is $(x000000)_2$, size is 32B (no footer in this example)

→ p's buddy is 32 B block begins at $x000000 \wedge (1 < 5)$ which is $(x100000)_2$



Buddy system

`p = malloc(1)`

`free(p)`

p's address is $(x000000)_2$, size is 32B

→ p's next block address is $p + 32B$
which is $(x100000)_2$

Free lists

2^4

2^5

2^6

$(x000000)_2$

